Skill-Biased Structural Change*

Francisco J. Buera  
Federal Reserve Bank of Chicago  
Joseph P. Kaboski  
University of Notre Dame  
Richard Rogerson  
Princeton University  
August 21, 2015

Abstract

We document for a broad panel of advanced economies that increases in GDP per capita are associated with a systematic shift in the composition of value added to sectors that are intensive in high-skill labor, a process we label as skill biased structural change. It follows that further development in these economies leads to an increase in the relative demand for skilled labor. We develop a two-sector model of this process and use it to assess the contribution of this process of skill-biased structural change to the rise of the skill premium in both the US, and a broad panel of advanced economies, over the period 1977 to 2005. We find that these compositional changes in demand account for between 25 and 30% of the overall increase of the skill premium due to technical change.

*We thank Daron Acemoglu, David Dorn, Chad Jones, Pete Klenow as well as seminar participants at the 2015 AEA Meetings, Chicago Fed, Paris School of Economics, Pittsburgh, Stanford, University of Houston, and USC for useful comments.
1 Introduction

The dramatic increase in the wages of high skilled workers relative to low skilled workers is one of the most prominent secular trends in the US and other advanced economies in recent decades. Isolating the underlying causes of this trend is important for projecting future trends and evaluating the extent to which policies might be effective or advisable. The literature has consistently concluded that skill-biased technological change (SBTC) is a quantitatively important driver of the increase in the relative demand for high skilled workers. \(^1\)

In this paper we argue that a distinct process – which we label skill-biased structural change – has also played a quantitatively important role. We use the term skill-biased structural change to describe the systematic reallocation of sectoral value-added shares toward high-skill intensive industries that accompanies the process of continued development among advanced economies.

The economic intuition behind our result is simple. If (as we show is indeed the case in the next section) the process of development is systematically associated with a shift in the composition of value added toward sectors that are intensive in high-skill workers, then the demand for high-skilled workers will increase, independently of whether development is driven by skill-neutral or skill-biased technical change. This channel is absent in analyses that adopt an aggregate production function, since in that case development that comes from skill-neutral technical change has no effect on the relative demand for high-skilled workers.

To assess the quantitative significance of this channel, we develop a simple general equilibrium model of structural transformation that incorporates an important role for skill and use it to study the evolution of the US economy between 1977 and 2005. In order to best highlight the shift in value added to high skill-intensive sectors, we study a two-sector model in which the two sectors are distinguished by their intensity of skill workers in production. We allow for sector-specific technological change, which is a (sector-specific) combination of skill-neutral and skill-biased technical change. We show how the model can be used to infer preference parameters and the process for technical change using data on the change in the composition of employment by skill, the change in aggregate output, changes in sectoral factor shares, the skill premium, relative sectoral prices and the distribution of sectoral value added.

In the data, our measure of the skill premium increases from 1.41 to 1.90 between 1977 and 2005, an increase of 49 percentage points. \(^2\) Our calibrated

---

1Important early contributions to the literature on the skill premium that stress skill biased technical change include Katz and Murphy (1992), Bound and Johnson (1992), Murphy and Welch (1992), Berman et al. (1994) and Berman et al. (1998). This is not to say that SBTC is the only factor at work, as the literature has also highlighted the effect of other factors on overall wage inequality. For example, DiNardo et al. (1996) argue that labor market institutions such as minimum wages and unionization have played an important role in shaping wage inequality overall, Feenstra and Hanson (1999) emphasize the role of offshoring, and Autor et al. (2013) emphasize the role of trade.

2Our measure of the skill premium compares those with at least college degrees to those with high school degrees or less, and is based on total compensation and not just wages and
model perfectly matches this increase. We then use the model to decompose this increase into three different components: one due to the changes in the relative supply of high-skill workers, one part that is due to skill-biased technical change, and a third part due to other technological changes. If there had been no change in technology, our model predicts that the skill premium would have decreased to 0.92, a drop of 49 percentage points, due to the increase in the relative supply of high-skill workers. It follows that overall changes in technology created an increase in the skill premium of 98 percentage points. In our benchmark specification, between one quarter and one third of this increase comes from changes in technology other than skill-biased technical change, operating through their effect on the composition of value added. We conclude that systematic changes in the composition of value added associated with the process of development are an important factor in accounting for the rise in the skill premium. In fact, if skill-biased technical change had been the sole source of technical change over this period, our model predicts that the skill premium would have increased by only 18 percentage points instead of by 49.

Having established the importance of this effect for the US, we repeat the analysis for a set of nine other OECD countries. While there is some variation in the contribution of compositional changes in value added to changes in the skill premium across countries, ranging from around 10 percent to slightly more than 50 percent, the average for this sample is slightly above 30 percent, very much in line with our estimates for the US.

Our paper is related to many others in two large and distinct literatures, one on SBTC and the skill premium and the other on structural transformation. Important early contributions to the literature on the skill premium include Katz and Murphy (1992), Bound and Johnson (1992), Murphy and Welch (1992), Berman et al. (1994) and Berman et al. (1998). Given that the increase in the skill premium occurred in the face of a large increase in the supply of high skill workers, all of these papers sought to identify factors that would increase the relative demand for high-skilled workers. In addition to skill-biased technological change, each of them noted compositional changes in demand as a potentially important element of the increased relative demand for skill. Relative to them, our contribution is fourfold. First, we document the importance of compositional effects that are systematically related to the process of development. Second, we show how to uncover the different dimensions of technological change in a multi-sector framework. Third, we present a general equilibrium model in which one can assess the driving forces behind compositional changes. Fourth, and perhaps most importantly, our structural approach finds a much larger role for compositional effects.

An early contribution in the second literature is Baumol (1967), with more recent contributions by Kongsamut et al. (2001) and Ngai and Pissarides (2007). (See Herrendorf et al. (2014) for a recent overview.) Relative to this literature our main contribution is to introduce heterogeneity in worker skill levels into the analysis and to organize industries by skill intensity rather than broad sectors.
The paper that we are most closely related to is Buera and Kaboski (2012). Like us, they study the interaction between development and the demand for skill, though their primary contribution is conceptual, building a somewhat abstract model to illustrate the mechanism. Relative to them our main contribution is to build a simple model that can easily be connected to the data and to use the model to quantitatively assess the mechanism. Leonardi (forthcoming) considers a similar mechanism to us, but focuses on how demand varies by education attainment as opposed to income more broadly, and finds relatively small demand effects. An important antecedent of our work is the paper by Acemoglu and Guerrieri (2008). Like us, they study the relationship between development and structural change in a model that features heterogeneity in factor intensities across sectors. But differently than us, they focus on differential intensities for physical capital and the role of the relative price of physical capital rather than human capital. Their work is also primarily theoretical.

An outline of the paper follows. Section 2 presents aggregate evidence on the relation between development and the value added share for high skill intensive services in a panel of advanced economies, in addition to some other important empirical patterns. Section 3 presents our general equilibrium model and characterizes the equilibrium. Section 4 shows how the model can be used to account for the evolution of the US economy over the period 1977 to 2005, and in particular how the data can be used to infer preference parameters and the process of technical change. Section 5 presents our main results about the contribution of various factors to the evolution of the skill premium. Section 6 assesses the contribution of skill-biased structural change for relative prices, and in Section 7 we extend our analysis to a set of nine other countries. Section 8 concludes.

2 Empirical Motivation

This section documents the prominence of what we refer to as skill-biased structural change, as well as some of its salient features. In particular, using data for a broad panel of advanced economies, we document two key facts. First, there is a strong positive correlation between the level of development in an economy, as measured by GDP per capita, and the share of value added that is attributed to high skill services. Second, there is also a strong positive correlation between the level of development and the price of high skill services relative to other goods and services. Interestingly, these relationships are very stable across countries, and in particular, the experience of the US is very similar to the average pattern found in the data.

We supplement the above aggregate time series evidence for a panel of countries with some evidence about cross-sectional expenditure shares in the US economy. In particular, we show that the expenditure of higher income house-

---

Ngai and Petrongolo (2014) use a similar framework to show that compositional changes in value added associated with development can explain part of the decrease in the gender wage gap that has occurred in the US over time.
holds contains a higher share of high skill intensive value-added. This fact will serve two purposes. First, it is suggestive evidence for a non-homotheticity in the demand for high skill services, which is a feature we will include in our model. Second, this cross-sectional moment provides important information about preference parameters that is not readily available from aggregate time series data.

2.1 Aggregate Panel Evidence

The starting point for our analysis is the earlier work of Buera and Kaboski (2012). They divide industries in the service sector into two mutually exclusive groups: a high skill intensive group and a low skill intensive group, and show that whereas the value added share of the high skill intensive group rose substantially between 1950 and 2000, the value added share of the low skill intensive group actually fell over the same time period. This finding suggests that the traditional breakdown of economic activity in the structural transformation literature, into agriculture, manufacturing and services, is perhaps not well suited to studying the reallocation of economic activity in today’s advanced economies. Here we pursue this line of work further, modifying their aggregation procedure to include goods-producing industries, and extending their analysis to a broad panel of advanced economies.

The analysis is based on value added data from the EUKLEMS Database (“Basic Table”). These data exist in comparable form for a panel of 12 advanced economies over the years 1970-2005. The sectoral value-added data are available at roughly the 1 to 2-digit industry level. We focus on a two-way split of industries into high skill intensive and low skill intensive based on the share of labor income paid to high-skill workers. While one could imagine more detailed splits, including more than two skill categories and perhaps interacting skill intensity with goods vs. services, we feel that this two-way split both facilitates exposition and allows us to capture a robust pattern in the cross-country data.

The labor payment data come from the EUKLEMS Labour Input Data and are slightly more disaggregated. High skill-intensive service sectors are: “Financial Intermediation”, “Real Estate and Business Services”, “Education”, and “Health and Social Work”. In 1970, the economy-wide average share of labor compensation paid to high-skill workers in the U.S. was 20 percent; the corresponding shares for these high skill-intensive industries were 34, 38, 74, and 49 percent, respectively. These industries remain well above average throughout the time period. We combine these data with real (chain-weighted) GDP per

---

4See O’Mahony and Timmer (2009).
5These countries are Australia, Austria, Denmark, France, Germany, Italy, Japan, the Netherlands, South Korea, Spain, the United Kingdom, and the United States. The U.S. data for value-added go back to only 1977, while the Japan data go back to only 1973.
6High-skill is defined as a college graduate and above.
7The next highest industries are “Chemicals and Chemical Products” (27 percent), “Coke, Refined Petroleum, and Nuclear Fuel” (21 percent), and “Electrical and Optical Equipment” (21 percent).
capita data from the Penn World Tables 7.1. Finally, we demean both the value-added share data and the (log) GDP per capita data by taking out country fixed effects.

\[
y = 0.17 \ln(x) - 1.37 \quad R^2 = 0.80
\]

\[
y = -0.17 \ln(x) + 2.37 \quad R^2 = 0.80
\]

Figure 1: Value-added by Skill-intensity and Economic Development.

Figure 1 shows the data pooled across time and countries. The small squares show the relationship for the panel of advanced countries; we have highlighted the United States data using the larger circles. The relationship is clear: the value added share of the high skill-intensive sector increases with log GDP/capita, with a highly significant (at a 0.1 percent level) semi-elasticity of 0.17. The regression line implies an increase of roughly 24 percentage points as we move from a GDP per capita of 10,000 to 40,000 (in 2005 PPP terms), and explains 80 percent of the variation in the data. Moreover, we see that the United States data is quite similar to the overall relationship. Indeed, the tight relationship suggests that cross-country differences in the details for funding of education or health, for example, are second order relative to the income per capita relationship in terms of their effects on time series changes. In sum, the tendency for economic activity to move toward high skill-intensive services as an economy develops is a robust pattern in the cross-country data.

One of the common explanations for structural change is changes in relative prices. (See, for example, Baumol (1967) and Ngai and Pissarides (2007).) Using value-added price indices from the same EUKLEMS Database, we can examine the correlation between the relative price of high-skill intensive services and the increasing value added share of high-skill intensive services that accompanies
the process of development. Figure 2 is analogous to Figure 1, but it plots the price index of the high skill-intensive sector relative to the low-skill intensive sector rather than share data on the y-axis. Again we have demeaned both the relative price and log GDP per capita data to eliminate country fixed effects, and normalized the relative price indices to 100 in 1995. As before, the larger circles represent the U.S. data.

\[
y = 51.9 \ln(x) - 428.2 \\
R^2 = 0.84
\]

Figure 2: Relative Price of Skill-intensity Sector and Economic Development.

Again, the relationship is striking. The linear regression is highly significant, explains 84 percent of the variation in the demeaned data, and is quantitatively important: the relative price of the high skill-intensive sector increases almost two and a half times over the range of the data. Finally, the U.S. relationship is quite similar to the overall relationship, and again the tight relationship suggests that cross-country variation in this relative price-income relationship is second order. We conclude that changes in relative prices are another robust feature of the structural transformation process involving the movement of activity toward the high-skill intensive sector.

2.2 Income Effects: Cross-Sectional Household Evidence

A second common explanation for structural change is income effects associated with non-homothetic preferences. (See, for example, Kongsamut et al. (2001).) With this in mind it is of interest to ask whether high-skill intensive services are...
a luxury good, i.e., have an income elasticity that exceeds one. To pursue this we examine whether the relationship between the skill intensity of value-added consumption and income exists in the expenditure data from a cross-section of households. To the extent that all households face the same prices at a given point in time and have common preferences (or at least preferences that are not directly correlated with income), the cross-sectional expenditure patterns within a country abstract from the relative price relationship in Figure 2 and allow us to focus on the effect of income holding prices constant.

One complication with pursuing this approach is that it involves mapping household expenditure data through the input-output system in order to determine the consumption shares of value added. We briefly sketch the steps of this procedure here, and provide more details in the appendix. We start with the household level Consumer Expenditure Survey (CEX) data for the United States from 2012. We adapt a Bureau of Labor Statistics mapping from disaggregated CEX categories to 76 NIPA Personal Consumption Expenditure (PCE) categories. We then utilize a Bureau of Economic Analysis (BEA) mapping of these 76 PCE categories to 69 input-output industries that properly attributes the components going to distribution margins (disaggregated transportation, retail, and wholesale categories). Using the 2012 BEA input-output matrices, we can then infer the quantity of value added of each industry embodied in the CEX expenditures. We classify the 69 industries as high skill intensive or low skill intensive using the EUKLEMS data as previously noted.\(^9\)

This procedure generates household-level data for the share of total expenditure that represents valued added by high skill intensive sectors and low skill intensive sectors, which we can regress on household observables, most importantly income or education, and potentially a host of other household level controls. We restrict ourselves to the primary interview sample, and each observation is a household-month observation.

Table 1 presents results for regressions of the total share of expenditures that is high skill intensive. The first column presents results from an OLS regression on log after tax income and a set of demographic controls, including age, age squared, dummies for sex, race, state, urban, and month, and values capturing household composition (number of boys aged 2-16, number of girls aged 2-16, number of men over 16, number of women over 16 years, and number of children less than 2 years). The coefficient on log income in the first column indicates that the semi-elasticity of the share of value-added embodied in expenditures is 0.012.

Income is certainly mis-measured in the micro data, and even if properly measured it would only proxy for permanent income, leading to a likely attenuation bias. The second column attempts to alleviate this measurement error by instrumenting for log income using the years of schooling attained by the head of household. Instrumenting for income in this fashion increases the coefficient roughly four-fold to 0.049.

\(^9\)The labour data from EUKLEMS contains 41 distinct industries. The "basic" data, from which we obtain value-added data, contain only 33 distinct industries.
Table 1: Household High-Skill Intensive Expenditure Share vs. Income

<table>
<thead>
<tr>
<th></th>
<th>OLS</th>
<th>IV</th>
<th>OLS</th>
</tr>
</thead>
<tbody>
<tr>
<td>Ln Income</td>
<td>0.012***</td>
<td>0.049***</td>
<td>.</td>
</tr>
<tr>
<td>SE</td>
<td>0.001</td>
<td>0.002</td>
<td>.</td>
</tr>
<tr>
<td>High Skill Head</td>
<td>.</td>
<td>.</td>
<td>0.043***</td>
</tr>
<tr>
<td>SE</td>
<td>.</td>
<td>.</td>
<td>0.002</td>
</tr>
<tr>
<td>$R^2$</td>
<td>0.08</td>
<td>0.02</td>
<td>0.15</td>
</tr>
<tr>
<td>Observations</td>
<td>48,550</td>
<td>48,550</td>
<td>17,812</td>
</tr>
</tbody>
</table>

*** indicate significance at the 1 percent level.

Controls include: age; age squared; dummies for sex, race, state, urban, and month; number of boys (2-16 year); number of girls (2-16 years); number of men (over 16 years); number of women (over 16 years); and number of infants (less than 2 years).

High skilled is defined as 16 years of schooling attained, while low skilled is defined as 12 years attained.

The last column uses education as a direct regressor, replacing log income with a dummy for whether the head of household is high skilled or not. Here high skill is defined as having exactly 16 years of education, while low skill is defined as having exactly 12 years. (The rest of the households are dropped, leading to the smaller sample.) The coefficient indicates that the share of value-added embodied in expenditures is 4.3 percentage points higher in households with a high-skilled head.

We have examined the robustness of the results in Table 1 along various dimensions. Table 1 uses monthly expenditures of the household, but if we aggregate household expenditures across the three months they are surveyed, we find nearly identical results. By defining high skill as those with at least 16 years of education, and low skill as those with less than 16 years of education, we expand the sample somewhat, but the raw estimates are similar (0.032 rather than 0.043).\textsuperscript{10} Dropping demographic controls increases the sample by about 15 percent and lowers the coefficients on income by roughly 50 percent, but the coefficients remain highly significant. Dropping the controls has essentially no impact on the high-skilled head of household coefficient. The main effect of dropping the controls is substantially lower $R^2$ values.

Quantitatively, even the larger, instrumented, income coefficient of 0.049 is substantially smaller than the aggregate time series value of 0.17 in Figure 1, but not negligible in comparison. We therefore take this as suggestive evidence that, in addition to relative prices, non-homotheticities may also play a role in accounting for the observed pattern of skill-biased structural change.

Lastly, we note an important limitation in directly applying the micro elas-

\textsuperscript{10}If we directly estimate expenditure elasticities by regressing the (log) level of high skill intensive value-added on the (log) level of expenditures gives substantially higher estimates. This is driven by certain lumpy expenditures like higher educational expenses and car purchases driving both up in particular months. This motivates our emphasis on the relationship between the high skill intensive share and education or income rather than direct expenditures per se.
ticity as an income effect. Because the CEX captures only out-of-pocket expenditures, it underestimates the true consumption of certain goods like insurance premiums (a substantial share of which is paid by employers) and higher education (a substantial share of which is paid by government).\footnote{The estimated income semi-elasticity of the share of out-of-pocket insurance is actually significantly negative in the CEX data although overall insurance consumption is certainly positive. Similarly, although the expenditure share-income semi-elasticity of higher education is positive, it is likely understated. Finally, the lack of primary and tertiary expenditures may actually be overstated in the CEX data because it neglects public expenditures, but we conjecture that this relationship is small relative to the higher education relationship.}

### 2.3 Summary

In summary, we have documented a robust relationship in the time series data for advanced economies regarding the movement of activity into high-skill intensive services and the process of development. We refer to this process as skill-biased structural change, so as to emphasize both its connection to the traditional characterization of structural change and the special role of skill intensity. This relationship is remarkably stable across advanced economies, thus suggesting that it is explained by some economic forces that are robustly associated with development, with country specific tax and financing systems not playing a central role in explaining the time series changes.

In documenting this relationship we have used a two-way split into high and low skill intensive sectors. This masks important within sector heterogeneity. Indeed, within the low skill intensive sector, a pattern emerges that the relatively more skill intensive sectors within this category, e.g., manufacturing industries like electrical equipment and chemicals, expand relative to the less skill intensive sectors like agriculture or textiles.\footnote{Katz and Murphy (1992) give a detailed analysis across 150 2-digit industry-occupation cells for the period, 1963-1987. Autor and Dorn (2013) present a recent account focusing on detailed occupation categories.} In this sense, our simple dichotomy may understate the true extent of skill biased structural change. However, the relative price patterns, use patterns (consumption and investment), and trade patterns make the analysis at a more disaggregated level more difficult to interpret and much less directly tied to traditional structural change forces.

The traditional structural transformation literature emphasizes the role of both non-homotheticities and relative price changes as drivers of structural change, and we have also presented evidence that both of these effects are relevant in the context of skill-biased structural change as well. Specifically, we documented a strong positive correlation between the relative price of high skill intensive services and GDP per capita in a cross-country panel as well as a positive correlation between household value added expenditure shares on high skill intensive services and income in the US cross-section. These relationships are not only highly statistically significant, but they are also economically significant in a quantitative sense.
3 Model and Equilibrium

Our analysis emphasizes how intratemporal equilibrium allocations are affected by changes in the economic environment that operate through changes in income and relative prices. To capture these interactions in the simplest possible setting, we adopt a static closed economy model with labor as the only factor of production. Our model is essentially a two-sector version of a standard structural transformation model extended to allow for two labor inputs that are distinguished by skill. In this section, we describe the economy and its equilibrium at a point in time; later we describe the features that we will allow to change over time to generate skill-biased structural change as described in the previous section.

3.1 Model

There is a unit measure of households. A fraction $f_L$ are low-skill, and a fraction $f_H$ are high skill, where $f_L + f_H = 1$. All households have identical preferences defined over two commodities. In our empirical analysis these two commodities will be connected to the low and high skill intensive aggregates studied in the previous section. As a practical matter, all of our high skill intensive sectors are services and all goods sectors are in the low skill intensive sector. It is notionally convenient to label the two commodities as goods and services even though what we label as goods includes low-skill services.

We assume preferences take the form:

$$
\alpha_G c_{Gi}^{\varepsilon} + (1 - \alpha_G) (c_{Si} + \bar{c}_S)^{\varepsilon-1}
$$

where $c_{Gi}$ and $c_{Si}$ are consumption of goods and services by an individual of skill level $i$, $0 < \alpha_G < 1$, $\bar{c}_S \geq 0$ and $\varepsilon > 0$. Note that if $\bar{c}_S > 0$, preferences are non-homothetic and, holding prices constant, the expenditure share on services will be increasing in income. This non-homotheticity is motivated by the cross-sectional analysis in the previous section. Note that households are assumed to not value leisure, since our focus will be on the relative prices of labor given observed supplies.

Each of the two production sectors has a constant returns to scale production function that uses low- and high-skilled labor as inputs. We assume that each of these production functions is CES:

---

13 This is a simple and common way to create differential income effects across the two consumption categories. One can also generate non-homothetic demands in other ways. For example, Hall and Jones (2007) generate an income elasticity for medical spending that exceeds unity through the implied demand for longevity. Boppart (2014), Swiecki (2014) and Comin et al. (2015) all consider more general preferences with the common feature being that income effects associated with non-homotheticities do not vanish asymptotically. This property is likely to be relevant when considering a sample with countries at very different stages of development. Because we focus on a sample of predominantly rich countries, we have chosen to work with the simpler preference structure in order to facilitate transparency of the economic forces at work.
\[ Y_j = A_j \left[ \alpha_j \frac{H_j}{\rho_j} + (1 - \alpha_j) \frac{L_j}{\rho_j} \right]^{\frac{\rho_j}{\rho_j - 1}} j = G, S \]

where \( L_j \) and \( H_j \) are inputs of low- and high-skilled labor in sector \( j \), respectively. The parameter \( \alpha_j \) will dictate the importance of low- versus high-skilled labor in each sector. While one could imagine that the elasticity of substitution between these two factors also differs across sectors, our benchmark specification will assume that this value is the same for both sectors. We consider the effects of cross-sectional variation in this parameter in our sensitivity analysis.

Before proceeding to analyze the equilibrium for our model we want to comment on the significance of abstracting from capital and trade. By excluding capital we implicitly adopt a somewhat reduced form view of skill-biased technological change. For example, changes in relative demand for skilled labor due to capital-skill complementarity and changes in the price of equipment (as in (Krusell et al., 2000), for example), will show up in our model as skill-biased technological change. While it is obviously of interest to understand the underlying mechanics of skill-biased technological change, for our purposes we believe our results are strengthened by adopting a more expansive notion of skill-biased technological change rather than focusing on a specific mechanism.

While we abstract from trade, we believe our analysis is largely complementary to those that emphasize the role of trade in shaping the evolution of the skill premium. In particular, our analysis focuses on the extent to which compositional changes between goods and high-skill services diminish the role of skill-biased technological change in accounting for changes in the skill premium. To the extent that trade is dominated by trade in goods, it could diminish the role of skill-biased technical change by potentially affecting compositions within the goods sector. For example, if the US increasingly exported high skill-intensive manufactured goods and imported low skill-intensive manufactured goods, this would shift the composition of production within the goods sector, and will in our analysis be interpreted as skill-biased technological change within the goods sector. Put somewhat differently, we believe that trade may serve to generate a process of skill biased structural change within the goods sector, and in this sense represents an additional channel to the one that we focus on.

### 3.2 Equilibrium

We focus on a competitive equilibrium for the above economy. The competitive equilibrium will feature four markets: two factor markets (low- and high-skilled labor) and two output markets (goods and services), with prices denoted as \( w_L, w_H, p_G \) and \( p_S \). We will later normalize the price of low-skilled labor to unity so that the price of high-skilled labor will also represent the skill premium, though in our derivations it will be convenient to postpone implementing this normalization.

The definition of competitive equilibrium for this model is completely standard and straightforward, so here we focus on characterizing the equilibrium.
Individuals of skill \( i = L, H \) solve

\[
\max_{c_{Gi}, c_{Si}} \left( a_G c_{Gi}^{\frac{\varepsilon - 1}{\varepsilon}} + (1 - a_G) (c_{Si} + \bar{c}_S)^{\frac{\varepsilon - 1}{\varepsilon}} \right)
\]

subject to

\[
p_G c_{Gi} + p_S c_{Si} = w_i. \tag{1}
\]

The first-order conditions associated with this problem are:

\[
a_G c_{Gi}^{\frac{1}{\varepsilon}} = p_G \lambda_i \tag{2}
\]

\[
(1 - a_G) (c_{Si} + \bar{c}_S)^{\frac{1}{\varepsilon}} = p_S \lambda_i \tag{3}
\]

Rearranging these two first order conditions and substituting into (1) yields:

\[
c_{Gi} = \frac{w_i + p_S \bar{c}_S}{p_S \left( \left( \frac{1-a_G}{a_G} \right)^\varepsilon \right) + p_G}
\]

and

\[
c_{Si} = \frac{\left( \frac{1-a_G}{a_G} \right)^\varepsilon w_i - p_G \bar{c}_S}{p_S \left( \left( \frac{1-a_G}{a_G} \right)^\varepsilon \right) + p_G}
\]

Normalizing \( w_L \) to unity, the aggregate expenditure share for services is:

\[
\frac{p_S \left( (1 - f_H) c_{SL} + f_H c_{SH} \right)}{1 - f_H + f_H w_H} = \left( \frac{1-a_G}{a_G} \right)^\varepsilon
\]

\[
\frac{\left( \frac{1-a_G}{a_G} \right)^\varepsilon + \left( \frac{p_G}{p_S} \right)^{1-\varepsilon}}{1 - f_H + f_H w_H} - \frac{p_S \bar{c}_S}{1 - f_H + f_H w_H} \left( \frac{1-a_G}{a_G} \right)^\varepsilon + \left( \frac{p_G}{p_S} \right)^{1-\varepsilon} \tag{4}
\]

This expression is useful to illustrate the two forces driving structural change in the model, relative prices and income effects. Provided that \( \varepsilon < 1 \), as \( p_G/p_S \) declines, the share of services increases. Also, provided that \( \bar{c}_S \), as the income in units of services, \( (1 - f_H + f_H w_H)/p_S \), increases, the share of services grows.

The problem of the firm in sector \( j = G, S \) is

\[
\max_{H_j, L_j} p_j A_j \left[ \alpha_j H_j^{\frac{\varepsilon - 1}{\varepsilon}} + (1 - \alpha_j) L_j^{\frac{\varepsilon - 1}{\varepsilon}} \right]^{\frac{1}{\varepsilon}} - w_H H_j - L_j
\]

The first order conditions are

\[
p_j A_j \left[ \alpha_j H_j^{\frac{\varepsilon - 1}{\varepsilon}} + (1 - \alpha_j) L_j^{\frac{\varepsilon - 1}{\varepsilon}} \right]^{\frac{1}{\varepsilon}} (1 - \alpha_j) L_j^{\frac{1}{\varepsilon}} = 1 \tag{5}
\]

\[
p_j A_j \left[ \alpha_j H_j^{\frac{\varepsilon - 1}{\varepsilon}} + (1 - \alpha_j) L_j^{\frac{\varepsilon - 1}{\varepsilon}} \right]^{\frac{1}{\varepsilon}} \alpha_j H_j^{\frac{1}{\varepsilon}} = w_H \tag{6}
\]
Taking the ratio of (5) and (6) we obtain

\[ \frac{H_j}{L_j} = \left( \frac{1}{1 - \alpha_j w_H} \right)^\rho \]  \tag{7}

Substituting (7) into (5) and rearranging delivers an equation for the price of sector \( j \) output in terms of the skill premium \( w_H \):

\[ \hat{p}_j (w_H) = \frac{1}{A_j} \left[ \frac{\alpha_j}{w_H} + (1 - \alpha_j) \right]^{\frac{1}{1-\rho}}. \]  \tag{8}

The above expression implies that the search for equilibrium prices can be reduced to a single dimension: if we know the equilibrium wage rate for high-skilled labor then all of the remaining prices can be determined.

Finally, we derive an expression for the market-clearing condition for high-skilled labor that contains the single price \( w_H \). Using (7), the production function of sector \( j \), and (8), we obtain a sector-specific demand function for high-skilled labor:

\[ H_j = \left[ \frac{\alpha_j \hat{p}_j (w_H) A_j}{w_H} \right]^\rho Y_j A_j, \]  \tag{9}

which, together with equilibrium in the goods market, yields the market-clearing condition for high-skilled labor solely as a function of \( w_H \):

\[ \left[ \frac{\alpha_S \hat{p}_S (w_H) A_S}{w_H} \right]^\rho \sum_{i=L,H} f_i \hat{c}_{Si} (w_H) \]  
\[ + \left[ \frac{\alpha_G \hat{p}_G (w_H) A_G}{w_H} \right]^\rho \sum_{i=L,H} f_i \hat{c}_{Gi} (w_H) = f_H. \]  \tag{10}

Here we have used \( \hat{c}_{ji} (w_H) \) to denote the demand for output of sector \( j \) by a household of skill level \( i \) when the high-skilled wage is \( w_H \) and prices are given by the functions \( \hat{p}_i (w_H) \) defined in (8).

### 4 Accounting for Growth and Structural Transformation

In this section we calibrate the model of the previous section so as to be consistent with observations on structural transformation, growth, and the skill premium under the assumption that the driving forces are changes in technology (both skill-biased and skill-neutral) and changes in the relative supply of skill. In particular, we will use the above model to account for observed outcomes at two different points in time, that we denote as 0 and \( T \) for the initial and terminal periods respectively. Consistent with the existing literature on technological change and the skill premium, we do not allow the parameter \( \rho \) to change over time. We also assume that preferences are constant over time.
4.1 Targets for Calibration

Calibrating the model in the initial and terminal period requires assigning values for 14 parameters. Nine of these are technology parameters: 4 values of the $a_j$ (two in each period), 4 values of the $A_j$ (two in each period), and $\rho$. Three are preference parameters: $\varepsilon$, $a_G$ and $\bar{c}_S$. Last we have the value of $f_H$ at the two dates. The two initial values of the $A_j$ represent a choice of units, reducing the overall number of parameters to be set to twelve. In our benchmark specification we will set the two elasticity parameters $\rho$ and $\varepsilon$ based on existing estimates, further reducing this number to ten.

As described below, we will directly measure the initial and final values of $f_H$ from the data. To calibrate the remaining parameters we will target the following values which reflect the salient features of growth, structural transformation and demand for skill: the initial and final values for factor shares in both sectors, the initial and final value added shares for the two sectors, the initial and final value of the skill premium, the change in the relative price of the two sectors, and the overall growth rate of the economy.

In choosing values for these targets we rely on the EUKLEMS data from Section 2. For the U.S., complete data are available for the years 1977 to 2005, so we choose these two years as our initial and terminal year respectively. This period is of interest, since 1977 effectively marks a local minimum in the skill premium (see (Acemoglu and Autor, 2011) for earlier data), and it secularly increases after 1977.

Many of the values for targets have direct counterparts in the data and so require no discussion, but the construction of targets for the labor variables does merit some discussion. The data contain total compensation and total hours by industry, skill level (“low”, “medium”, and “high”, which are effectively, less than secondary completion, secondary completion but less than tertiary completion, and four year college degree or more), gender, and age groupings (15-29, 30-49, and 50 and over). Consistent with our calculations in Section 2, we combine the compensation of EUKLEMS categories of “low” and “medium” educated workers of all genders and ages into our classification of low-skilled, and “high” educated workers into our classification of high-skilled, in order to calculate labor income shares by skill at both the aggregate and sectoral level. We use the same sectoral classification as in Section 2.

Setting targets for the skill premium and the relative supply of skilled workers requires that we decompose factor payments into price and quantity components. If all workers within each skill type were identical then we could simply use total hours as our measure of quantity, but given the large differences in hourly wage rates among subgroups in each skill type this seems ill-advised. Instead, we assume that each subgroup within a skill type offers a different amount of efficiency units per hour of work. We normalize efficiency units within each

---

14BEA data on value added and prices are also available for the period 1977-2007 and line up quite closely with the KLEMS data. The BEA data does not allow consistent aggregation prior to 1977. Data on labor compensation and hours are only available through 2005, which is why we choose 2005 as our terminal date.
skill type by assuming one hour supplied by a high school-educated ("medium") prime-aged (i.e., aged 30-49) male is equal to one efficiency unit of low skill labor and that one hour supplied by a college-educated ("high") prime-aged (i.e., aged 30-49) male is equal to one efficiency unit of high skill labor. \(^{15}\) With this choice of units, the skill premium is defined as the ratio of college-educated ("high") to high school-educated ("medium") prime-aged (i.e., aged 30-49) male wages. This premium rises from 1.41 in 1977 to 1.90 in 2005. \(^{16}\)

Finally, we infer \(f_H\) using the identity that the ratio of labor compensation equals the product of the skill premium and the relative quantity of high- to low-skilled labor (\(f_H = 1 - f_L\), respectively). Equivalently, one could compute efficiency units of each skill type by using relative wages within each skill group to infer efficiency units and directly aggregating efficiency units. Note that our implicit assumption is that differences in wages between different low-skilled (high-skilled) demographic groups reflect differences in efficiency units of low-skilled (high-skilled) labor. This procedure implies that high skill labor was 22% of total labor supply in 1977 and rose to 34% in 2005. (For comparison, the fraction of raw hours that were high skill labor increased from 18% to 31% over the same time.)

Table 2 summarizes the values used for the targets listed above.

<table>
<thead>
<tr>
<th>(f_{H0})</th>
<th>(f_{HT})</th>
<th>(w_{H0})</th>
<th>(w_{HT})</th>
<th>(% \Delta \frac{w_H}{w_L})</th>
<th>(% \Delta Y)</th>
<th>(\theta_{G0})</th>
<th>(\theta_{GT})</th>
<th>(\theta_{S0})</th>
<th>(\theta_{ST})</th>
<th>(\frac{C_{G0}}{Y_{G0}})</th>
<th>(\frac{C_{ST}}{Y_{ST}})</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.22</td>
<td>0.34</td>
<td>1.41</td>
<td>1.90</td>
<td>62.0</td>
<td>70.0</td>
<td>0.18</td>
<td>0.34</td>
<td>0.54</td>
<td>0.66</td>
<td>0.29</td>
<td>0.44</td>
</tr>
</tbody>
</table>

4.2 The Calibration Procedure

Having described the targets to be used in the calibration and the data used to determine the values of these targets, we now describe the details of the mapping from targets to parameters. We proceed in two steps. The first step shows how the technology parameters are inferred. In the second step, we describe how to infer values for the preference parameters.

We begin with the determination of technological change. First, we show that given a value for \(\rho\), the four values of the \(\alpha_{jt}\) are pinned down by sectoral

\(^{15}\)While one could obviously normalize units by choosing other reference groups, this group seems most natural since its uniformly high rate of participation over time minimizes issues associated with selection.

\(^{16}\)Comparing earnings of full time workers using CPS data, Figure 1 in Acemoglu and Autor (2011) indicates values of 1.39 and 1.64 for 1977 and 2005 respectively. Our measure indicates a roughly 25 percentage point greater increase. This difference reflects two factors. First, although our lower skill group includes those with some college education, our high skill group includes those with post-graduate education, for whom wage growth has been dramatic. Autor et al. (2008) find 31 percentage points log wage growth for those with 18+ years of education between 1979-2005 relative to 18.5 for those with 16 or 17 years. Second, our measure is based on total compensation and not just on labor earnings. Pierce (2010) documents that the change in the 90-10 ratio over this time period is more than twenty log points higher when using total compensation than when using CPS wages. His analysis is based on firm level data and so does not allow a breakdown by educational attainment.
factor income shares and the skill premium, $w_{Ht}$. To see this, note that the share of sector $j$ income going to high skill labor is

$$\theta_{Hjt} = \frac{w_{Ht}H_{jt}}{\bar{p}_j(w_{Ht})Y_{jt}} = \frac{\alpha_{jt}^p}{\alpha_{jt}^p + (1 - \alpha_{jt})^p w_{Ht}}$$

where the second line follows from equations (8) and (9). Therefore, given $\rho$, the skill premium $w_{Ht}$, and data for $\theta_{Hjt}$, the value of the $\alpha_{jt}$ are given by:

$$\alpha_{jt} = \frac{1}{1 + \frac{1}{w_{Ht}} \left( \frac{1 - \theta_{Hjt}}{\theta_{Hjt}} \right)^\frac{1}{\rho}}.$$

Next we turn to determining the values of the $A_{jt}$’s. As noted previously, the two values in period 0 basically reflect a choice of units and so can be normalized. We will normalize $A_{S0}$ to equal one, and given the calibrated values for the $\alpha_{j0}$ and the value of $w_{H0}$, we choose $A_{G0}$ so as to imply $p_{G0}/p_{S0} = 1$. In this case $p_{GT}/p_{ST}$ can be easily identified with the change in the relative sectoral prices. As is well known in the literature, with identical Cobb-Douglas sectoral technologies, relative sectoral prices are simply the inverse of relative sectoral TFPs, so the change in relative prices would therefore determine the values of the two $A_{jt}$’s up to a scale factor.\footnote{This same relation holds more generally, and in particular would also apply if the sectoral production functions are CES with identical parameters.} This precise result does not apply to our setting because of sectoral heterogeneity in the $\alpha_{jt}$’s. (The skill premium also plays a role in determining relative prices, which we examine in Section 6.) Nonetheless, there is still a close connection between relative sectoral prices and relative sectoral TFPs (i.e., the $A_{jt}$). In particular, using equation (8) for the two sectors we have:

$$\frac{A_{Gt}}{A_{St}} = \frac{p_{St}}{p_{Gt}} \left[ \frac{\alpha_{Gt}^p}{w_{Gt}} + (1 - \alpha_{Gt})^p \right]^{1/(1 - \rho)} \left[ \frac{\alpha_{St}^p}{w_{St}} + (1 - \alpha_{St})^p \right]^{1/(1 - \rho)}.$$

The scale factor will of course influence the overall growth rate of the economy between periods 0 and $T$, so we choose this scale factor to target the aggregate growth rate of output per worker.\footnote{Note that to compute aggregate output at a point in time (and thus also the growth rate in aggregate output) it is necessary to know the sectoral distribution of output. The relations imposed thus far guarantee that maximum profits will be zero in each sector but do not determine the scale of operation. Intuitively, the split of activity across sectors at given prices will be determined by the relative demands of households for the two outputs. Below we will describe how preference parameters can be chosen to match the sectoral distribution of value added at both the initial and final date. At this stage we simply assume this split is the same as in the data.}
To this point, given a value for $\rho$, we have identified all of the technology parameters. For our benchmark analysis we set $\rho = 1.42$, which corresponds to the value used in Katz and Murphy (1992), and which is commonly used in the literature. Though this is a commonly used value in the literature, it is worth noting that previous estimates using an aggregate production function do not necessarily apply in our setting. For this reason we will also do sensitivity analysis with regard to $\rho$ over a fairly wide interval, ranging from 0.77 to 2.50. Table 3 below shows the implied values for the technology parameters.

Table 3

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value 1</th>
<th>Value 2</th>
<th>Value 3</th>
<th>Value 4</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\alpha_{G0}$</td>
<td>0.28</td>
<td>0.55</td>
<td>0.43</td>
<td>0.66</td>
</tr>
<tr>
<td>$\alpha_{S0}$</td>
<td>1.25</td>
<td>2.27</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\alpha_{ST}$</td>
<td>0.37</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$A_{ST}/A_{S0}$</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$A_{GT}/A_{G0}$</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

A few remarks are in order. Not surprising given the way in which we grouped industries into the two sectors, the weight on low-skilled labor is greater in the goods sector than in the service sector at both dates. More interesting is that in both sectors technological change has an important component that is skill biased. While the level drop in $\alpha$ is larger for the goods sector than the service sector, the percent changes are very similar, though slightly larger for the service sector than the goods sector (22% versus 20%). It follows that the extent of skill biased technological change is relatively similar for the two sectors.

However, overall technological progress is much greater in the goods sector than in the service sector. The TFP term in the goods sector more than doubles between 1977 and 2005, corresponding to an average annual growth rate of 2.97%. In contrast, the growth of the TFP term in the service sector averages only 0.80% per year.

We now turn to the issue of determining the values for the three preference parameters: $a_G$, $c_S$ and $\varepsilon$. While technological change can be inferred without specifying any of the preference parameters, we cannot evaluate some of the counterfactual exercises of interest without knowing how relative demands for the sectoral outputs are affected by changes in prices. As noted above, the calibration of technology parameters used information about sectoral expenditure shares without guaranteeing that observed expenditure shares were consistent with household demands given all of the prices. Requiring that the aggregate expenditure share for goods (or services) is consistent with the observed values in the data for the initial and terminal date would provide two restrictions on the three preference parameters. It follows that we would either need to introduce an additional moment from the data, or perhaps use information from some outside study to determine one of the three preference parameters. As noted earlier, for our benchmark results we will follow the second approach and fix the value of $\varepsilon$, and then use data on aggregate expenditure shares to pin down the values for $a_G$ and $c_S$. Our main finding is relatively robust to variation over a large range of values of $\varepsilon$, thereby lessening the need to tightly determine its value. Nonetheless, in Section 5 we will describe how cross-sectional data
on expenditure shares could be used as an additional moment and allow us to
determine all three preference parameters.

The empirical literature provides estimates of $\varepsilon$ that correspond to the
categories of “true” goods and “true” services, but not for our definitions of the
two sectors that are based purely on skill intensity. The key distinction is that
we have grouped low-skill services with goods. However, given that our goods
sectors does contain all of the industries that produce goods, while our service
sector does consist entirely of service sector industries, it seems reasonable that
information about the elasticity of substitution between the true goods and
services sectors should be informative about the empirically plausible range of
values for $\varepsilon$ in our model. Recalling that the objects in our utility function reflect
the value-added components of sectoral output, the relevant estimates in the lit-
erature would include Herrendorf et al. (2013), Buera and Kaboski (2009), and
Swiecki (2014). All of these studies suggest very low degrees of substitutability
between true goods and true services. For this reason we consider values for $\varepsilon$
in the set $\{0.125, 0.20, 0.50\}$, with $\varepsilon = 0.20$ chosen as our benchmark.$^{19}$

Given a value for $\varepsilon$, equation (4) can be used to determine values for $a_G$ and
$\bar{c}_S$ if we require that the model match the initial and final sectoral value added
shares.

Table 4 shows the values for the preference parameters in the different sce-
narios.

<table>
<thead>
<tr>
<th>$\varepsilon$</th>
<th>$a_G$</th>
<th>$\bar{c}_S$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Benchmark</td>
<td>0.20</td>
<td>0.72</td>
</tr>
<tr>
<td>High $\varepsilon$</td>
<td>0.50</td>
<td>0.31</td>
</tr>
<tr>
<td>Low $\varepsilon$</td>
<td>0.125</td>
<td>0.92</td>
</tr>
</tbody>
</table>

The qualitative patterns in this table are intuitive. Note that in each case
the changes in income, relative prices and the aggregate expenditure shares are
the same. As we move from $\varepsilon = 0.20$ to $\varepsilon = 0.125$ we decrease the elasticity
of substitution between the two goods, implying a smaller response in relative
quantities but a larger response in relative expenditure shares. In order to
compensate for this larger effect, we need to decrease the impact of income
changes on relative expenditure shares, implying a lower value for $\bar{c}_S$. The
lower value for $\bar{c}_S$ will in turn lead to a higher expenditure share on services in
the initial period, since the non-homotheticity is now less important. Hence, in
order to match the expenditure shares for the initial period we need to attach
a lower weight, $a_G$, to consumption of goods. As we move from $\varepsilon = 0.20$ to
$\varepsilon = 0.50$ we see the reverse pattern.

$^{19}$Comin et al. (2015) redo the exercise in Herrendorf et al. (2013) for a more general class
of preferences and find an elasticity of substitution that is somewhat higher, though still less
than 0.50, which is our upper range.
5 Decomposing Changes in the Skill Premium

Our model is calibrated so as to account for the observed change in the skill premium between 1977 and 2005. In this section we use the calibrated model to perform counterfactuals that allow us to attribute changes in the skill premium to the various exogenous driving forces in the model. Our primary objective is to decompose the effect of changes in technology on the skill premium into a piece due to skill biased technological change and a residual piece that is due to other forms of technological change. The residual piece affects the relative demand for skilled individuals indirectly, through its impact on the relative consumption of services.

Table 5 reports the results of our counterfactual exercises for each of the three specifications that differ with respect to the value of \( \varepsilon \). As we will see, the key results are very similar across the three specifications, so to better focus our discussion we will concentrate on the \( \varepsilon = .20 \) case and later summarize the other cases.

The first two rows of the table report the starting and ending values for the skill premium, which are the same in our model as they are in the data. The rest of the table decomposes this change into several pieces by considering several counterfactual exercises in our model. The first counterfactual assesses the role of “supply” versus “demand” factors. Specifically, the share of labor supply coming from skilled workers increases between 1977 and 2005, and in the absence of any other changes exerts downward pressure on the skill premium. As noted above, focusing on the \( \varepsilon = .20 \) case for now, the third row of Table 5 shows that if the change in relative supply of skill (i.e., the \( f_i \)'s) had been the only change between 1977 and 2005 the skill premium would have decreased from 1.41 to 0.92, a decrease of 49 percentage points. Given that we in fact observe a increase in the skill premium of 49 percentage points, it follows that the overall effect of technological change is to increase the skill premium by 98 percentage points.

Our next goal is to decompose the 98 percentage point increase in the skill premium due to the overall effect of technological change into one part that is due to skill biased technological change (i.e., changes in the \( \alpha_{jt} \)'s) and a second part due to other dimensions of technical change (i.e., changes in the \( A_{jt} \)'s).

There are two natural calculations that one could perform to assess the contribution of changes in the \( A_{jt} \)'s to changes in the skill premium. In both
calculations we start from the previous counterfactual in which we change only the supply of skill. In the first calculation we add in the change in the $A_{jt}$'s and compute the fraction of the overall 98 percentage point increase that they account for. In the second calculation we instead add in the changes in the $\alpha_{jt}$'s and compute the fraction of the 98 percentage point increase that is not accounted for. In a linear model these two calculations would give the same answer, but to the extent that nonlinearities are present they may differ. It will turn out that the answers do differ, but only to a relatively minor extent.

The final two rows in Table 5 present the results of these two calculations. Specifically, moving from the third row to the fourth row we see that the change in the $A_{jt}$'s increases the skill premium from 0.92 to 1.16, an increase of 24 percentage points. This represents roughly 24 percent of the overall 98 percentage point increase accounted for all technical change. Moving from the third row to the fifth row, we see that the changes in the $\alpha_{jt}$'s cause the skill premium to increase from 0.92 to 1.59. The residual is 31 percentage points, which represents approximately 31% of the 98 percentage point increase due to all changes in technology. Based on this we conclude that non-skill biased technical change accounts for between 25 and 30 percent of the overall change in the skill premium due to technical change. Put somewhat differently, according to our calibrated model, if skill biased technical change had been the only force affecting the relative demand for skill then the skill premium would have increased by only 18 percentage points instead over the period 1977 to 2005 instead of increasing by 49 percentage points.

If we redo these calculations for the other two values of $\varepsilon$ the answers are similar. For $\varepsilon = 0.50$ the two methods imply that changes in the $A_{jt}$'s account for 22% and 31% of the overall change in the skill premium due to technical change, whereas for $\varepsilon = 0.125$ the two values are effectively identical to those for the $\varepsilon = 0.20$ case, being equal to 24% and 31%. From this we conclude that our finding of a significant contribution of changes in the $A_{jt}$'s is robust to a large variation in the value of $\varepsilon$.

In the introduction we stressed the fact that aggregate production function analyses abstract from compositional changes, and that our main objective was to assess the quantitative importance of the compositional changes that are associated with the process of structural transformation during development. The previous calculations decomposed the overall changes in the skill premium into parts due to skill-biased technological change and skill-neutral technological change. In order to make the connection between this decomposition and compositional changes it is of interest to examine the connection between technological change and changes in sectoral value added shares. Table 6 reports the results for each of the three values of $\varepsilon$.
Table 6
Technical Change and Value Added Share of Skill-Intensive Services
US, 1977-2005

<table>
<thead>
<tr>
<th></th>
<th>$\varepsilon = 0.50$</th>
<th>$\varepsilon = 0.20$</th>
<th>$\varepsilon = 0.125$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Model 1977</td>
<td>0.29</td>
<td>0.29</td>
<td>0.29</td>
</tr>
<tr>
<td>Model 2005</td>
<td>0.44</td>
<td>0.44</td>
<td>0.44</td>
</tr>
<tr>
<td>Model 2005 with fixed $A_j$</td>
<td>0.26</td>
<td>0.25</td>
<td>0.25</td>
</tr>
<tr>
<td>Model 2005 with fixed $\alpha_j$</td>
<td>0.44</td>
<td>0.46</td>
<td>0.46</td>
</tr>
</tbody>
</table>

The first two rows of the table remind us that the (skill-intensive) service sector grew significantly between 1977 and 2005, increasing its share of value added from 29 percent to 44 percent. Recall that our calibrated model perfectly replicates the change in the data. The last two rows provide two different ways of assessing the role of changes in the $A_j$’s and the $\alpha_j$’s in accounting for this compositional change. The third row reports the service sector value added share that would have resulted if the changes in the change in the $\alpha_{jt}$’s had been the only source of technological change, whereas the fourth row reports the service sector value added share that would have resulted if the change in the $A_{jt}$’s had been the only source of technological change. Both calculations lead to the same conclusion: effectively all of the compositional change is accounted for by changes in the sectoral TFPs. It follows that our previous decomposition of changes in the skill premium due to the two different sources of technical change can effectively be interpreted as statements about the importance of structural change.

Non-skill biased technological change in our model still has two distinct dimensions: one which increases the overall level of TFP in the economy and the other of which increases relative TFP in the goods sector. As we noted above, both of these changes tend to reallocate activity from the goods sector to the service sector, thereby indirectly increasing the relative demand for skill. Next we examine the relative magnitude of these two effects.

Note that for given changes in the $A_{jt}$’s the relative magnitude of these two effects is dictated by the preference parameters $\varepsilon$ and $\bar{c}_S$: as $\varepsilon$ becomes smaller, relative TFP changes have larger effects, and as $\bar{c}_S$ becomes larger then sector neutral changes in the $A_{jt}$’s have larger effects. Because our calibration procedure implies that as $\varepsilon$ becomes smaller the value of $\bar{c}_S$ decreases, we expect to find that sector neutral change plays a larger role for smaller values of $\varepsilon$.

To evaluate this we consider the counterfactual in which we hold all parameters fixed from the original calibration, allow the $f_{it}$’s and the $\alpha_{jt}$’s to change as before, but counterfactually force the $A_{jt}$’s to grow at the same rate, with this rate chosen so as to yield the same overall change in aggregate output as in the data. When we do this, the implied values of the skill premium are 1.83, 1.72, and 1.69 for the cases of $\varepsilon = 0.50$, 0.20, and 0.125 respectively. It follows that when $\varepsilon = 0.50$ it is income effects that dominate the overall impact of the $A_{jt}$’s on the skill premium, whereas for the smaller values of $\varepsilon$ the sector biased nature of TFP growth is somewhat more important than the income effect. So while the three different specifications offer very similar decompositions regarding the
overall effect of changes in the $A_{jt}$’s on the skill premium, they have distinct implications for how different type of changes in the $A_{jt}$ lead to changes in the skill premium.

5.1 Using Data to Infer $\varepsilon$

In the results above we considered a range of values for $\varepsilon$ rather than trying to use our model to infer a specific value. Since our main message was robust to a wide range of values for $\varepsilon$ we do not view this is a particular limitation of the analysis. Nonetheless, in this subsection we describe how the use of a cross-sectional moment on the household side would allow us to also infer a value for $\varepsilon$.

Intuitively, cross-sectional information can provide information about the magnitude of the income effect: assuming that all households have the same preferences and face the same prices at a point in time, cross-sectional heterogeneity in income will allow us to infer the size of the income effect. This can be implemented using the cross-sectional information that we reported in Section 2. In particular, our empirical analysis found that the expenditure share for services is 0.04 higher for high skill households than for low skill households. If we require that our model match this moment in the final time period, the implied values for $\varepsilon$ and $\bar{c}_S$ are 0.05 and 0.08 respectively when we assume $\rho = 1.42$. This would correspond to values of $\varepsilon$ somewhat below the lower end of the interval that we considered. As a practical matter, it turns out that moving to increasingly smaller values of $\varepsilon$ from $\varepsilon = 0.20$ has relatively small effects, as could already be seen in Table 4. We have also repeated this exercise for values of $\rho$ equal to 0.77 and 2.50 and obtained estimates of $\varepsilon = 0.11$ and 0.01 respectively. While we do not report the results for these cases in detail, we note that our main message remains unaffected if we were to adopt these specifications.

Having offered the idea of using cross-sectional data to infer the size of income effects on the demand for what we have labelled goods and services, we think it is important to repeat one important limitation of this approach in the current context. Two of the largest components of high skill services are education and health care, both of which are not well tracked by household expenditure surveys. To the extent that spending on some components of education and health reflect a collective societal choice, it is not clear that cross-sectional data will be useful in detecting how cross-sectional differences in income affect desired consumption.

5.2 Sensitivity Exercises

For the results in the previous section we assumed that $\rho = 1.42$, which we noted was a standard value in the literature, and the value implied by the analysis in Katz and Murphy (1992). However, we also noted that the aggregate analyses that have supported this estimate are not necessarily appropriate in our multi-sector economy. For this reason we also consider a wider range of values for $\rho$.
to assess the extent to which the above conclusions are robust to variation in this parameter.

We consider two alternative values of \( \rho \), corresponding to higher and lower elasticities of substitution. Specifically, we consider \( \rho = 0.77 \) and \( \rho = 2.5 \). In each case we redo the calibration procedure as before. While the value of \( \rho \) does affect the quantitative findings, it leaves our main message largely unchanged. For example, focusing on the case of \( \varepsilon = 0.20 \) we find that when \( \rho = 0.77 \), the share of changes in the skill premium due to technical change that are accounted for by changes in the \( A_j \) is 27% and 41% from the two methods. When \( \rho = 2.50 \) the corresponding values are 19% and 23%. We conclude that our main finding of a significant role for changes in demand composition induced by technical change in accounting for changes in the skill premium is robust to considering a wide range of values for \( \rho \), though higher values of this elasticity parameter do lead to modest declines in the estimated role played by demand composition.

Our analysis has assumed that the value of \( \rho \) is the same in both sectors. Absent any empirical evidence on the extent of heterogeneity in \( \rho \) across sectors, this seemed a natural benchmark. Reshef (2013) suggests that the elasticity of substitution between high and low-skilled workers may be lower in services, for example. It is therefore important to assess whether our results are sensitive to the assumption of \( \rho \) being constant across sectors. To do this we redo our exercise for several specifications in which we allow the two values of \( \rho \) to vary across sectors, allowing for the ratio \( \frac{\rho_G}{\rho_S} \) to be both larger and smaller than one. In all cases we assume that the weighted average of the two elasticities—\( (H_G/H)\rho_G + (H_S/H)\rho_S \)—is equal to 1.42 when evaluated at the initial factor shares, so that our analysis can be interpreted as assessing the effect of heterogeneity holding the aggregate elasticity of substitution constant. We consider values for \( \rho_S \) of 0.77, 0.91, 1.11, and 2.00, and the implied values for \( \rho_G \) are 2.23, 2.06, 1.82, and 0.73. Table 7 reports the same statistics as in Table 5, focusing on the case of \( \varepsilon = 0.20 \).

<table>
<thead>
<tr>
<th>Table 7</th>
<th>The Effect of Sectoral Variation in ( \rho )</th>
</tr>
</thead>
<tbody>
<tr>
<td>US, 1977-2005</td>
<td>( \frac{\rho_G}{\rho_S} = 0.35 )</td>
</tr>
<tr>
<td>( w_{HT} )</td>
<td>1.41</td>
</tr>
<tr>
<td>( w_{HT} )</td>
<td>1.90</td>
</tr>
<tr>
<td>Counterfactual ( w_{HT} )</td>
<td></td>
</tr>
<tr>
<td>changes in:</td>
<td>1.00</td>
</tr>
<tr>
<td>( f_i ) only</td>
<td>1.15</td>
</tr>
<tr>
<td>( f_i ) and ( A_j ) only</td>
<td>1.66</td>
</tr>
</tbody>
</table>

For ease of comparison, the fourth column repeats the results from our benchmark specification. For values of \( \rho_S/\rho_G < 1 \) the implications are affected very little, and to the extent that a very large value of \( \rho_S/\rho_G \) influences the quantitative results, it yields a larger role for the demand side effects that we focus on (between 31% and 42%). Noting that we are considering a very wide range
of variation in the relative values of $\rho$, we conclude that our results are quite robust to variation in $\rho$ across sectors.

Lastly, we consider the extent to which mis-measurement of relative prices might influence our results. Our quantitative analysis utilized information about changes in the relative price of the high skill intensive sector. Between 1977 and 2005 this relative price increased by more than sixty percent. One possible concern is that price inflation in the high skill intensive sector might be upward biased because of the failure to properly account for quality improvements.

Here we report the results of a simple exercise to assess the extent to which our conclusions are affected by this possibility. In particular, consider the case in which the true increase in the relative price of the high skill intensive sector was only half as much as indicated by the official data. This means that real value added in this sector increased by roughly 30% more than indicated by the official data, and aggregate GDP grew by roughly 15 additional percentage points. We set $\rho = 1.42$ and $\varepsilon = 0.20$ and carry out the same calibration procedure as previously. Not surprisingly, given that we are holding $\varepsilon$ fixed and decreasing the role of relative price changes, the calibration procedure yields a larger value for $\varepsilon s$, indicating a larger role for nonhomotheticities. However, we find that the contribution of demand factors is virtually identical to what we found in our benchmark calculation. So while mismeasurement of relative price changes has implications for relative magnitudes of preference parameters, it has virtually no effect on our assessment of the role of demand factors.

5.3 Comparison with Earlier Literature

The increase in the relative demand for high-skilled labor that we attribute to structural change is substantially higher than the overall effects of relative demand shifts found in the earlier literature on the topic. For example, in the overlapping years of our samples, 1979-1987, Katz and Murphy (1992, KM hereafter) attributed 4.6 percentage points of increase in relative demand for high-skilled labor to changes in industrial composition (i.e., their “between industry” analysis, see Table VIII), and they did so using a much more highly disaggregated industrial classification rather than our stark two-sector specification. This contributes only 11 percent of the increase in skill premium over that period, given their estimated elasticity of substitution and the increased supply over that period. Bound and Johnson (1992) estimate a small but slightly negative contribution of industrial composition. In contrast, when we restrict attention to the overlapping years 1979-1987, our simulations attribute between 22 and 27 percent of the increase in the skill premium to the increase in the relative demand of high-skilled labor associated with skill-biased structural change.

Note that our overall results are for a somewhat later period, 1977-2005 vs. 1963-1987, and our data are substantially more aggregated in terms of industry, educational attainment, and experience levels. Nonetheless, by focusing on overlapping years and conducting KM analyses on our data, we can show that the importance of these differences is quantitatively small and that two impor-
tant factors stand out in driving our substantially larger estimates for the role of changes in the composition of demand. (See Appendix for more details.)

First, KM’s decomposition using observed industrial movements is an approximation, which, as they acknowledge, underestimates the true contribution of demand shifts because the skill premium rose during the period of analysis. A rising skill premium disproportionately increases the price of the skill-intensive output (see equation (8)), reducing the movement of resources into that sector relative to what would be observed with perfectly elastic labor supply (i.e., the full shift in demand).\(^{20}\) Whereas they are able to analytically sign the bias, the added structure of our model enables us to actually quantify this bias. In addition, our analysis uses a global solution of the model, instead of a local approximation. For the years 1979-1987, our model attributes an increase in the skill premium of between 9 and 11 percentage points due to changes in relative demand for goods and services. This is larger than the 5 percentage point increase in the skill premium that we would attribute to changes in composition of demand using their methods on our simulated data.

Second, sectoral movements are more important in our analysis because of the way that we measure differences in skill intensity across sectors. Focusing on the EUKLEMS data, our method finds a 24 percentage point difference in factor intensities across our two sectors on average, in line with the difference in factor payments, while KM’s method finds only a 4 percentage point difference. To construct efficiency unit stocks from heterogeneous labor forces, the KM method is to construct labor stocks directly using only observed labor supply measures (i.e., number of body-hours by education, experience, gender weighted by their average relative wages across industries and time). This rules out unobserved variation in labor quality across industries and over time. In contrast, we impute our labor supply measures indirectly from data on relative wages and industry-specific factor payment shares. Effectively, factor payment shares vary substantially more across industry than the ratios of simple bodies of different types, so that average wages of observable groups also vary substantially across industries. Our analysis assumes that all labor is paid its marginal product. We therefore attribute the discrepancy in average wages across industries for observably similar labor types to unobserved quality differences. We rule out other sources like industry rents or compensating differentials, for example. Applying the KM local approximation together with the KM measures of efficiency units on our EUKLEMS data, we account for only a 2 percentage point increase in the skill premium due to changes in the composition of demand in this period. This is, slightly lower than their 5 percentage point increase because of our coarser observed grid on labor (18 types of labor rather than 320 types in KM).

In summary, there are two important factors that explain why we find a substantially larger role for compositional effects in accounting for increases in the skill premium relative to the earlier literature. The first is that our

\(^{20}\)Bound and Johnson adjust for the increase in relative supply of high-skilled labor without accounting for the fact that the relative wage nevertheless rose. This appears to account for their much lower estimate than KM.
structural approach allows us to precisely disentangle the role of different driving forces. The second is that we allow for differences in unobserved productivity for workers across sectors, which in turn implies larger differences in skill intensity across sectors, thereby increasing the potential impact of compositional changes on the relative demand for skill.

6 Decomposing Changes in Relative Prices

While our main focus has been to understand the relative importance of different factors in generating the observed changes in the skill premium, our model also allows us to assess the importance of different factors in generating the change in the relative price of skill intensive services over time. In particular, our model suggests two distinct channels at work. As is standard in the literature on structural change with uneven technological progress across sectors, differential growth in sectoral TFP will lead to changes in relative sectoral prices. But our model also features an additional channel: because the sectors have different factor shares, changes in the relative price of factors will also lead to changes in relative sectoral prices. In particular, since the high-skill intensive sector uses skilled labor more intensively, any increase in the relative price of skilled labor will lead to a higher relative price for this sector. This effect was previously documented in equation (8).21

Here we perform some counterfactuals in our benchmark specification (i.e., \( \rho = 1.42 \) and \( \varepsilon = 0.20 \)) to assess the relative importance of these two forces. In the data, the relative price of high-skill intensive services increases by 62 percentage points between 1977 and 2005, and by virtue of our calibration procedure, our model perfectly accounts for this increase. To assess the pure role played by the increase in the skill premium, we compute the implied relative price from equation (8) assuming that all technology parameters remain fixed at their 1977 values, but letting the skill premium increase from 1.41 to 1.90, as in the data. The result is an increase in the relative price of skill intensive services of 11 percentage points, or roughly 18% of the overall increase. In interpreting this magnitude it is important to recall our earlier discussion of the possibility that estimates of the change in relative prices are biased upward because due to a failure to properly control for quality increases in the service sector. If the true change in relative prices was indeed only half as large as in the data, then the change in the skill premium would account for 36% of the overall change. While still not the dominant factor, this suggests that changes in the skill premium may well be a significant factor behind changes in relative prices.

The issue of price mismeasurement notwithstanding, the direct effects of technological change are the dominant force behind the increase in the relative price of skill intensive services in our benchmark calibrated model. Moreover, it is the difference in sectoral TFP growth rates that drives this direct effect. To see this, take equation (8), hold the skill premium and sectoral TFPs constant

\[\text{Buera and Kaboski (2012) highlight this effect in a theoretical model in which the difference in skill-intensity across the goods and service sectors arises endogenously.}\]
and consider the pure effect of skill biased technological change. The result is that the relative price of skill intensive services would have decreased by 19 percentage points.

This last calculation examined the direct effect of changes in skill-biased technological change, but without incorporating the general equilibrium effect on wages. Our previous counterfactuals (see row 5 in Table 5) argued that if we eliminated changes in sectoral TFP, so that skill-biased technical change was the only source of technological change, the skill premium would have increased from 1.41 to 1.59. If we include this effect in combination with the direct effect of skill biased technological change, the result is that the relative price of skill intensive services decreases by 15 percentage points. We conclude that skill-biased technological change is not a source of increases in the relative price of services.

In summary, we conclude that although increases in the skill premium may directly account for a non-trivial share of the increase in the relative price of high-skill intensive services, the dominant factor behind this increase is the relatively slow sectoral TFP growth in this sector.

7 Cross Country Analysis

In this section we extend our analysis to nine other OECD countries for which the available data exists to address two distinct issues. The first issue concerns model validation, and the second issue is to assess the importance of skill-biased structural change for a larger set of countries.

7.1 Model Validation Using Cross-Country Data

Our calibration procedure assigned parameter values by targeting the same number of moments as there were parameters. While both the production structure and our method for inferring technological change are very standard, we inferred values for utility function parameters by requiring that the model match the beginning and final values for sectoral valued added shares. If our utility function were mis-specified in an important way, this procedure would still allow us to fit the initial and final sectoral value added shares, but in this case we might be wary of using our calibrated specification for the counterfactual exercises.

One simple test of the specification is to consider its ability to fit not only the two endpoints of our sample, but also the entire time series. Unfortunately this is not a very stringent test for the period we are studying, since the key series in our analysis are fairly linear, and the model is able to match them fairly well.

As a somewhat more stringent test, we turn to cross country data. For this exercise we use data from the following nine countries: Australia, Austria, Denmark, Germany, Italy, Japan, the Netherlands, Spain and the United Kingdom. We assume that the utility function for each country is the same as the one
implied by our benchmark calibration with $\rho = 1.42$ and $\varepsilon = 0.20$, i.e., we impose the implied values for $a_G$ and $\bar{c}_S$. Additionally, we assume that $\rho$ is the same for all countries. However, using the same procedures as earlier, for each country we measure the relative supply of skilled labor from the data and we use our model to infer the time series for technological change. Because preference parameters are imported from the calibration using US data, we have not imposed that the model will fit the time series of interest for each country. Nonetheless, Figure 3 shows that this specification provides a reasonably good fit to the actual data for this set of countries. Because the behavior of the skilled labor share and the skill premium do differ across countries, we believe that this finding is supportive of our parsimonious structure.\(^{22}\)

It is of interest to note that the above procedure implies processes for technological change that are broadly similar across countries, as shown in Figure 4.\(^{23}\) To the extent that we believe the process of technology adoption and diffusion are at least generally similar across rich countries, we would view it as somewhat problematic if our procedure indicated dramatically different processes across these countries.

\(^{22}\)We note that our model does not do such a good job of matching the series for Korea. Notably, it specifically fails for the early part of the sample in which Korea has very low GDP. We interpret this as evidence that our specification of non-homotheticities is probably best viewed as an approximation that holds in a restricted range of incomes, and that if one wants to consider a much larger range of incomes then it is probably important to consider more general specifications such as those in Boppart (2014) and Comin et al. (2015).

\(^{23}\)The plots in Figure 4 have removed country fixed effects in order to focus on the changes in technology over time rather than the cross-sectional differences.
Figure 4: Calibrated Technological Processes: Sector-Biased (left panel) and Skill-Biased (right panel) Technologies. The diamonds (squares) correspond to the high (low) -skill intensive sector.

7.2 Skill-Biased Structural Change and the Skill Premium in Cross Country Data

In this subsection we assess the extent to which skill biased structural transformation has influenced the skill premium in each of the countries studied in the previous subsection. We could carry out this calculation for the specifications in the last subsection, i.e., assuming the same preference parameters for these countries as in the US. A potential disadvantage of this method is that although the model with common preference parameters across countries offers a good fit to the cross country time series data, it does not necessarily account for all of the changes in the skill premium for each of the countries. Alternatively, we could assume country specific values for $\alpha_G$ and $\bar{c}_S$ and simply repeat the analysis that we have carried out for the US for each of the additional economies. These two methods provide fairly similar answers, and in the interest of space we only report the results of the second exercise, which are shown in Table 8.

To compute the values in Table 8 we first calculate the contribution of all forms of technological change by computing the difference between the actual skill premium in 2005 versus the skill premium that would have existed in 2005 if there had been no technological change relative to 1977 but allowing for the observed change in the supply of skill. We then isolate the fraction of this overall contribution of technological change that is due to skill biased structural change by computing the fraction of this change that is accounted for by changes in the $A_j$’s. Relative to our earlier calculations, this procedure corresponds to the change moving from row 3 to row 4 in Table 5.
### Table 8

<table>
<thead>
<tr>
<th>Country</th>
<th>Contribution of SBTC Across Countries</th>
</tr>
</thead>
<tbody>
<tr>
<td>Australia</td>
<td>0.18</td>
</tr>
<tr>
<td>Austria</td>
<td>0.40</td>
</tr>
<tr>
<td>Denmark</td>
<td>0.11</td>
</tr>
<tr>
<td>Spain</td>
<td>0.32</td>
</tr>
<tr>
<td>Germany</td>
<td>0.37</td>
</tr>
<tr>
<td>Italy</td>
<td>0.54</td>
</tr>
<tr>
<td>Japan</td>
<td>0.22</td>
</tr>
<tr>
<td>Netherlands</td>
<td>0.27</td>
</tr>
<tr>
<td>UK</td>
<td>0.36</td>
</tr>
</tbody>
</table>

The magnitude of this share varies significantly, from a low of 11% in Denmark to a high of 54% in Italy, but the mean value of 31% is very much in line with our estimates from the US. We conclude that the demand side forces associated with skill biased structural change seem to be quantitatively significant in a broad group of advanced economies.

## 8 Conclusion

Using a broad panel of advanced economies, we have documented a systematic tendency for development to be associated with a shift in value added to high-skill intensive sectors. It follows that development is associated with an increase in the relative demand for high skill workers. We coined the term skill-biased structural change to describe this process. We have built a simple two-sector model of structural transformation and calibrated it to US data over the period 1977 to 2005 in order to assess the quantitative importance of this mechanism for understanding the large increase in the skill premium during this period.

We find that technological change overall increased the skill premium by almost 100 percentage points, and that between 25 and 30 percent of this change is due to technological change which operated through compositional changes.

Our findings have important implications for predicting the future evolution of the skill premium, since the continued growth of the value added share of the high-skill intensive sector will exert upward pressure on this premium even in the absence of skill-biased technological change.

In order to best articulate the mechanism of skill-biased structural change we have purposefully focused on a simple two-sector model. As we noted in Section 2, there is good reason to think that the mechanism we have highlighted is also at work at a more disaggregated level, so it is of interest to explore this mechanism in a richer model. The early literature has also emphasized the possibility that increases in trade might lead to changes in the composition of valued added across sectors. Katz and Murphy (1992) specifically noted this possibility, and more recent analyses include Feenstra and Hanson (1999) and Autor et al. (2013). We think it is important to note that the compositional effects we have focused on are not likely to be reflecting changes due to trade.
The reason for this is that our high-skill intensive sector is composed entirely of industries from the service sector. It is plausible that part of what we identified as within sector skill biased technical change may at least in part reflect compositional effects due to trade, to the extent that trade had caused manufacturing activity in the US to shift to more skill intensive industries.
References


