

# Bitcoin's Fatal Flaw: The Limited Adoption Problem

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Does that fact arise from Bitcoin's infancy or structure?

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Economic Channel: Negative Network Effects

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Consensus: The network must agree on ledger contents

... that introduces a technical constraint (network delay)

Network delay contributes to negative network effects.

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- ▶ need for agreement on ledger contents (consensus)
- ▶ free entry (aka permissionless, “decentralized”)
- ▶ artificial supply constraint (BTC:  $\approx 10$  minute block times)

These features generate limited adoption.

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Fee increases expand the validator network (free entry)

Expanded network protracts consensus process

Prohibitive wait times result

Payment system viability relies on speed, so limited adoption arises

Fixed Supply + Free Entry + Consensus = Limited Adoption

## Decentralization implies Limited Adoption

Note: The aforementioned problem is artificial!  
i.e., block times are artificially constrained.

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Drawback: This solution succeeds only insofar as it induces centralization!

Arbitrarily fast block times cause delays to diverge purely due to the consensus process

Thus, even with dynamic block times, limited adoption obtains!

## A Solution: Public Permissioned Blockchain

A permissioned blockchain overcomes limited adoption by forgoing both free entry and fixed supply

Validator incentives, however, become relevant

Traditional voting schemes generate a co-ordination game with multiple equilibria, some undesirable

A stake-based voting scheme overcomes the limited adoption problem while precluding a bad co-ordination equilibrium

## Related Literature

### **Economic Limitations of Bitcoin**

Yermack (2015); Budish (2018); Biais, Bisiere, Bouvard, and Casamatta (2019); Foley, Hinzen, John and Saleh (2019); Saleh (2019b)

### **Alternative Protocols**

Bentov, Pass and Shi (2016); Chen and Micali (2016); Hinzen, Irresberger, John and Saleh (2019); Rosu and Saleh (2019); Russell, David, and Oliynykov (2017); Saleh (2019a)

### **Tokenomics**

Chod and Lyandres (2019); Cong and He (2019); Cong, Li and Wang (2019a); Cong, Li and Wang (2019b); Howell, Niessner, and Yermack (2019); Lee, Li, and Shin (2019); Lyandres (2019); Lyandres, Palazzo, and Rabetti (2019)

# Overview

## Two Types of Agents

- ▶ Validators (i.e., Miners)
- ▶ Users

## Two Types of Payment Systems

- ▶ Bitcoin
- ▶ Traditional Alternative

# Validators

Validators reference individual processors

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Validators (optimally) process fees in descending order

Validator sector is competitive so that:

$$V = \frac{\mathbb{E}[\sum f_i]}{\beta}$$

$\beta > 0$  denotes cost of a processor

# Users

User  $i$  receives utility  $R > 0$  if her transaction confirms

User  $i$  dislikes waiting and has time-sensitivity  $c_i \sim U[0, 1]$

User  $i$  dislikes having to pay a fee for processing

## User Problem

At  $t = 0$ , User  $i$  solves:

$$\max_{f_i \geq 0} R - c_i \cdot \mathbb{E}[W(f_i, f_{-i}) \mid c_i] - f_i$$

$W(f_i, f_{-i})$  denotes User  $i$ 's wait time given that she pays fee  $f_i$

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### Outside Option

If  $\max_{f_i \geq 0} R - c_i \cdot \mathbb{E}[W(f_i, f_{-i}) \mid c_i] - f_i < 0$  then User  $i$  does not transact via the blockchain

# Blockchain

A block is found when a validator solves a trivial puzzle.

Validators seek the puzzle solution via exhaustive enumeration.

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## Poisson Limit Theorem

if  $X_{i,n} \sim \text{Bernoulli}(p_n)$  i.d. and  $\lim_{n \rightarrow \infty} n \times p_n = \lambda$  then

$$\sum_{i=1}^n X_{i,n} \xrightarrow{d} \text{Poisson}(\lambda)$$

## Blockchain (Continued)

A validator's block finding process is (approximately) Poisson.

Independent Poisson processes sum to a Poisson Process.

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Previous papers assume blocks arrive according to a Poisson process.

This aggregation neglects network delay.

We augment that model to allow that disagreements arise from network delay.

Decker and Wattenhofer (2013) demonstrates that most Bitcoin disagreements arise precisely due to network delay.

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Disagreement occurs if one validator finds a block and then some other validator finds a block before hearing about the first block.

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$$p \equiv \mathbb{P}\{\text{No Disagreement}\} = \prod_i e^{-\lambda\Delta_i} = e^{-\Lambda\Delta}$$

$$\text{with } \Delta = \frac{1}{V} \sum_i \Delta_i \text{ and } \Lambda = \lambda V$$

## Network Delay

We let  $\Delta(V)$  denote the network delay of a network of size  $V$ .

Assumptions:

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Assumptions:

(1)  $\Delta(1) = 0$

(2)  $\lim_{V \rightarrow \infty} \Delta(V) = \infty$

(3)  $\Delta'(V) > 0$

(1) holds by definition; (2) holds by physical limitations.

(3) holds for PoW blockchains (see Chung and Lu (2002) and Riordan and Wormald (2010)).

## Equilibrium Conditions

- ▶ Users transact via the blockchain iff utility improving

$$\max_{f_i \geq 0} R - c_i \cdot \mathbb{E}[W(f_i, f_{-i}) \mid c_i] - f_i \geq 0 \Leftrightarrow \forall i : c_i \leq c^*.$$

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- ▶ Users select an optimal fee schedule

$$f_i \text{ solves } \max_{f_i \geq 0} R - c_i \cdot \mathbb{E}[W(f_i, f_{-i}) \mid c_i] - f_i \text{ if } c_i \leq c^*.$$

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$$f_i = 0 \text{ otherwise.}$$

- ▶ Validators earn no profits in equilibrium

$$\beta V = \mathbb{E}[\sum_i f_i].$$

# Equilibrium: Existence and Uniqueness

## Proposition

There exists an equilibrium. This equilibrium is unique among equilibrium with fee functions differentiable and increasing in wait dis-utility.

Note: This class of equilibria equates with that studied by Huberman, Leshno and Moallemi (2019)

## Demand and Validator Network Size

Increased Demand induces Higher Fees

Higher fees induce Validator Entry

More Formally,

### Lemma

$V$  increases in  $N$  and  $\lim_{N \rightarrow \infty} V_N = \infty$

## Expected Wait Time Decomposition

$$W_i = \frac{1}{\Lambda} + (N - 1) \frac{(c^* - c_i)}{\Lambda} + \tau(\Lambda, V)$$

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$(N - 1) \frac{(c^* - c_i)}{\Lambda}$  denotes expected wait for higher-priority users

$\tau(\Lambda, V)$  denotes expected disagreement resolution time

## Expected Wait Time Divergence

Increased demand leads to a more dispersed validator network. The more dispersed validator network induces more frequent disagreement. These disagreements delay consensus. In fact,

$$\lim_{N \rightarrow \infty} \tau(\Lambda, V_N) = \infty$$

Waits diverge even for the highest priority users!

$$\lim_{N \rightarrow \infty} \inf_i W_i = \infty$$

## An Adoption Problem

### Proposition

Adoption decreases as demand rises (i.e.,  $c^*$  decreases in  $N$ ). Moreover, the blockchain faces limited adoption (i.e.,  $c^* \rightarrow 0$ ).

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#### Increased Demand

- ⇒ Increased Fees
- ⇒ Larger Validator Network
- ⇒ Protracted Consensus Process
- ⇒ Prohibitive Delays
- ⇒ Limited Adoption

## Decentralization implies Limited Adoption

Why not relax the artificial supply constraint? (i.e., increase  $\Lambda$  with  $N$ )

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Even with a small network size, fast block times make consensus resolution diverge

Limited Adoption is overcome only if the network becomes centralized.

### Proposition

The blockchain necessarily faces either centralization (i.e.,  $V \rightarrow 1$ ) or limited adoption (i.e.,  $c^* \rightarrow 0$ ).

## Faster Blocks vs. More Disagreement

Speeding up the blockchain produces blocks faster but these blocks are also more likely to yield disagreement.

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Within Bitcoin's protocol, speeding up the blockchain produces exponentially more disagreement.

As such, speeding up the blockchain eventually increases wait-times and cannot overcome limited adoption without centralization

# Exponential Disagreement

Recall that agreement occurs with probability  $p = e^{-\lambda\Delta}$

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Thus, the likelihood of agreement decays exponentially in the block rate.

Expected Time to a Disagreement-Free Block:

$$\frac{1}{p \times \Lambda} = \frac{e^{\Lambda\Delta}}{\Lambda} \rightarrow \infty \text{ as } \Lambda \rightarrow \infty$$

# Buterin's Trilemma

**Blockchain Trilemma**

**Scalability**  
( Main Challenge )

The question is: How can we improve the scalability without reducing the security level and maintaining a decentral network on chain?

**Security**  
( Basic and Essential )

**Decentralization**  
( Core and Nature )

The diagram features a central triangle composed of several hexagonal blocks. The top block is orange and labeled 'Scalability (Main Challenge)'. The bottom-left block is teal and labeled 'Security (Basic and Essential)'. The bottom-right block is blue and labeled 'Decentralization (Core and Nature)'. The background is a dark teal with a network of white dots and lines.

## Significance of Network Delay

Network delay, an attribute of a distributed system and therefore a blockchain, serves as a critical factor for the results.

Absent network delay, the traditional solution of expanding supply to meet demand resolves the problem.

### Proposition

Both widespread adoption (i.e.,  $c^* \rightarrow \underline{c} > 0$ ) and decentralization (i.e.,  $V \rightarrow \infty$ ) can be obtained simultaneously under the counterfactual assumption of no network delay (i.e.,  $\Delta(V) = 0$ ).

## (Public) Permissioned Blockchain

Permissioned blockchains differ from Bitcoin by specifying a fixed set of validators.  
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This reduces the significance of network delay.

Permissioned Blockchains also remove the need for the Bitcoin puzzle which reduces wait times.

### Proposition

In any Permissioned Equilibrium, widespread adoption (i.e.,  $c^* \rightarrow \underline{c} > 0$ ) obtains.

## A Different Problem

Obtaining adoption for a permissioned blockchain is easy.

... but the purported advantage of Bitcoin-style blockchains is security not adoption.

Thus, the question becomes: are permissioned blockchains secure?

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This Paper: In general, No.

## Aside: Where's the Blockchain?

### Digital Signatures

- ▶ A valid block must be digitally signed by validators
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- ▶ The data structure uses hash-linking.
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### Hash-Linking

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- ▶ Hash-linking makes fraud detection trivial.

Validator identity is known, so reputation is particularly important.

# Equilibrium

$V_3$  plays H

		$V_2$	
		$H$	$M$
$V_1$	$H$	(0, 0, 0)	(0, $-\kappa$ , 0)
	$M$	( $-\kappa$ , 0, 0)	( $\Pi$ , $\Pi$ , 0)

$V_3$  plays M

		$V_2$	
		$H$	$M$
$V_1$	$H$	(0, 0, $-\kappa$ )	(0, $\Pi$ , $\Pi$ )
	$M$	(0, $\Pi$ , $\Pi$ )	( $\Pi$ , $\Pi$ , $\Pi$ )

$\kappa > 0$  represents a reputation cost.

$\Pi > 0$  represents a profit from malicious behavior.

H (M) represents Honest (Malicious) behavior.

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### Proposition

There exists no equilibrium in which an attack succeeds with strictly positive probability.

## Aside: Not Proof-of-Stake (PoS)

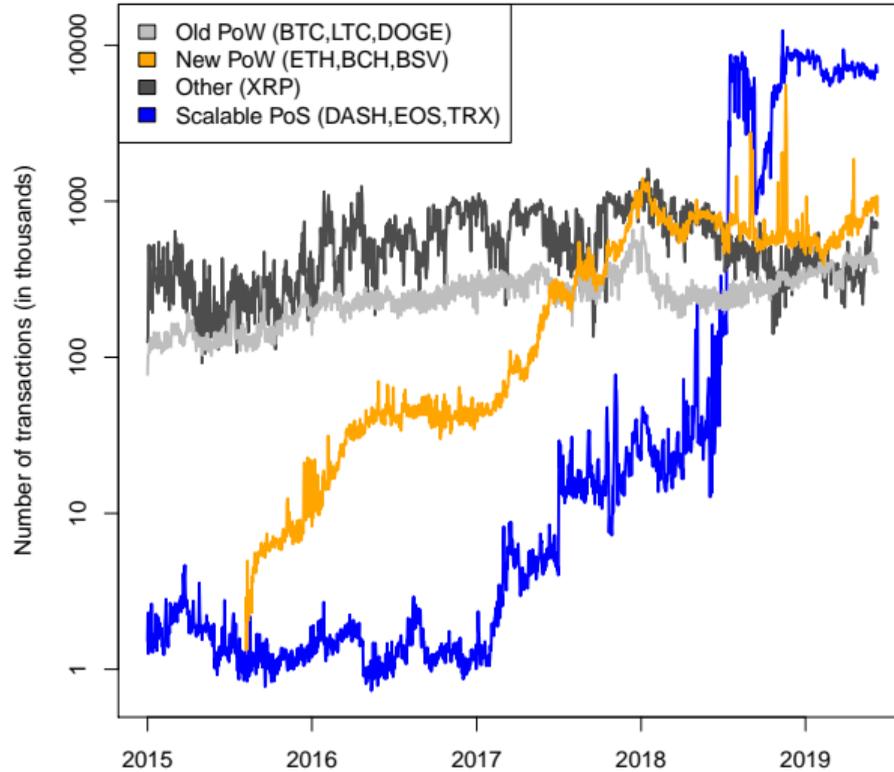
PoS allows any agent to participate in the validation process and therefore is permissionless.

Our proposed rule weights votes only among a specified permissioned set.

Our setting is permissioned with transparent identity - this creates an additional disincentive for malicious behavior arising from reputation costs.

# Conclusion

- ▶ Limited Adoption is endemic to Bitcoin.
- ▶ The traditional solution (i.e., increasing throughput) fails.
- ▶ More research is needed on alternatives...



Source: Hinzen, Irresberger, John and Saleh (2019)