# MAKING DECISIONS THAT REDUCE DISCRIMINATORY IMPACT

Matt J. Kusner

Chris Russell

Joshua R. Loftus

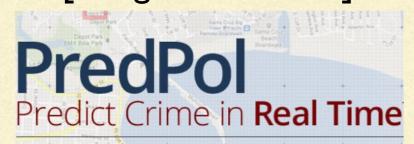
Ricardo Silva



# ML IS INVOLVED IN LIFE-CHANGING DECISIONS

## Policing

[Ensign et al., 2017]



### **Parole Sentencing**

[Larson et al., 2016]



# Advertising

[Sweeney, 2013]



Insurance

**H**<sub>2</sub>**O**.ai

Lending

:underwrite.ai

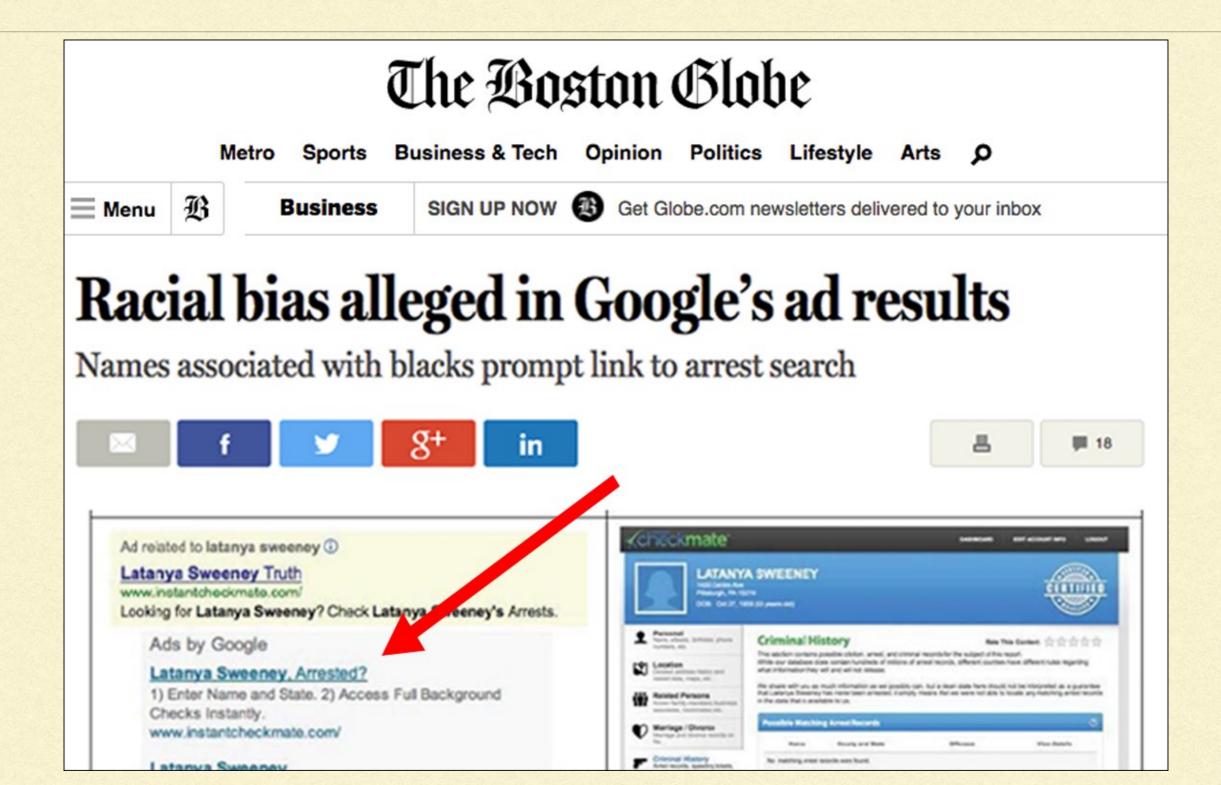
Insert your favorite application here!

# WE HAVE PROBLEMS



# ML CAN BE RACIST...

[SWEENEY, 2013]



# ML CAN BE SEXIST ...

[BOLUKBASI ET AL. 2016]



# DEFINITIONS OF FAIRNESS

Fairness Through Unawareness

Equality of
Opportunity
[Hardt et al., 2016]

Individual Fairness
[Dwork et al., 2012]

Demographic Parity [Zemel et al., 2013; Zliobaite, 2015]

Fair Calibration
[Pleiss et al., 2017]

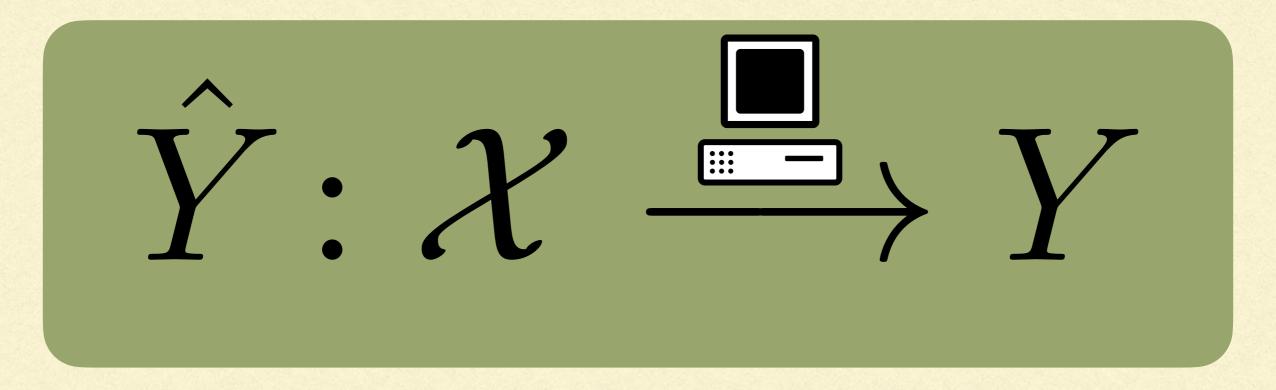
Preference Fairness
[Zafar et al., 2017]

Counterfactual Fairness
[Kusner et al., 2017]

Path-Specific Fairness
[Shpitser et al., 2017; Chiappa et al., 2018]

# PROBLEM #1

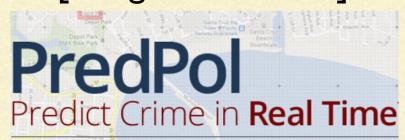
# The Discriminatory Prediction Problem



# ML IS INVOIVED IN LIFE-CHANGING DECISIONS

### Policing

[Ensign et al., 2017]



### **Parole Sentencing**

[Larson et al., 2016]



### Advertising



Insurance

Lending

H,O.ai :underwrite.ai

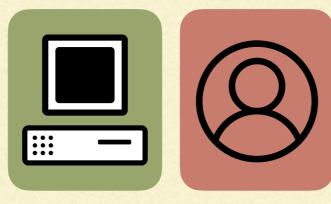
**Insert your** favorite application here!

# ML IS INVOLVED IN LIFE-CHANGING DECISIONS

### **Policing**



## **Parole Sentencing**



### Advertising



### Insurance





### Lending





Insert your favorite application here!

# ML IS INVOLVED IN LIFE-CHANGING DECISIONS

### **Policing**



impact: arrest

### **Parole Sentencing**



impact: jail-time

### **Advertising**



### Insurance



impact: improved health

### Lending

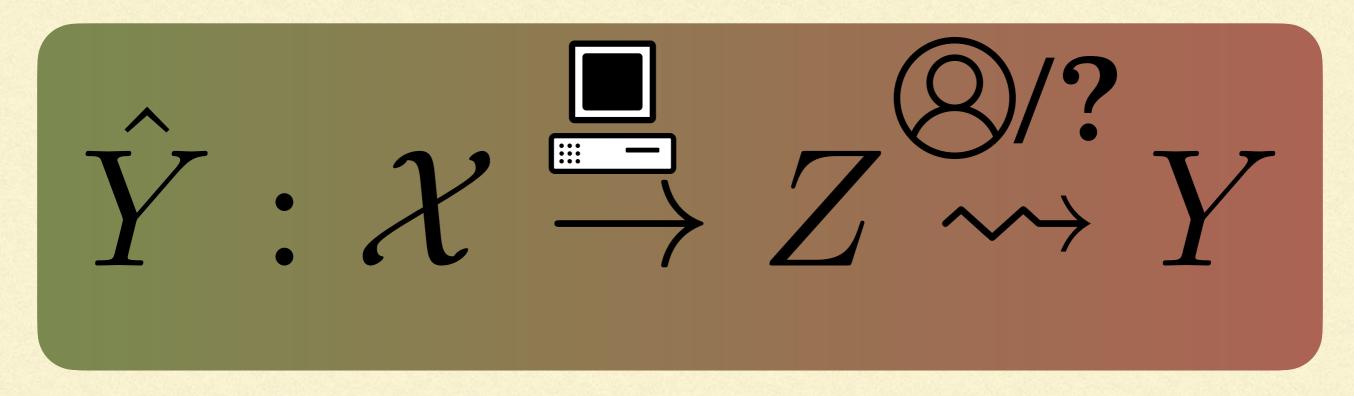


impact: pay off home loans

Insert your favorite application here!

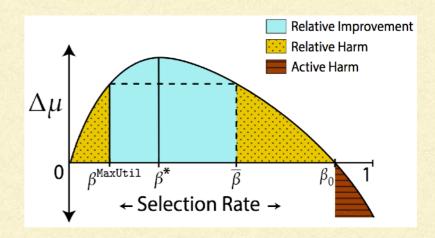
# PROBLEM #2

# The Discriminatory Impact Problem



# Introduction of discriminatory impact problem

[Liu et al., ICML 2018] [Green & Chen, FAT\* 2019]

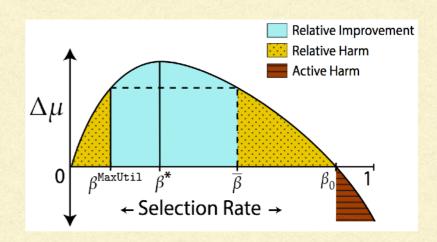


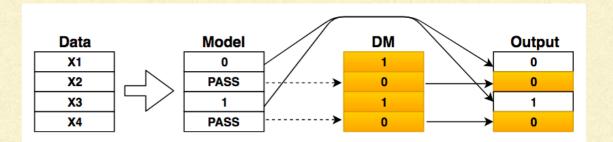
# Introduction of discriminatory impact problem

[Liu et al., ICML 2018] [Green & Chen, FAT\* 2019]

# Models for special cases

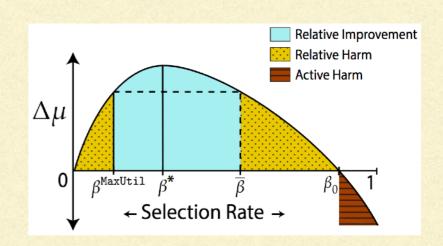
[Madras et al., NeurlPS 2018] [Kannan et al., FAT\* 2019]





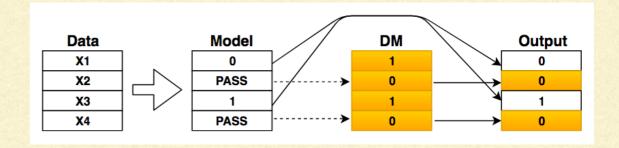
# Introduction of discriminatory impact problem

[Liu et al., ICML 2018] [Green & Chen, FAT\* 2019]



## Models for special cases

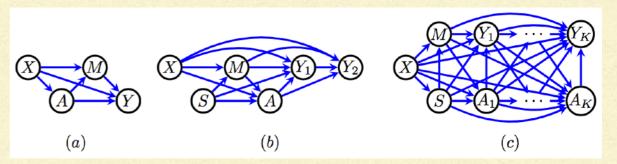
[Madras et al., NeurlPS 2018] [Kannan et al., FAT\* 2019]



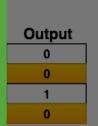
## Complimentary approaches

(RL, social dynamics)
[Nabi et al., ICML 2019]

[Hedari et al., ICML 2019]

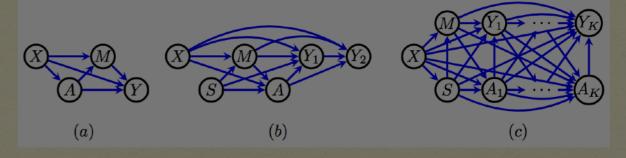


our work: a general framework for reducing discriminatory impact based on causal modeling and MILP



## Complimentary approaches

(social dynamics, RL) [Nabi et al., ICML 2019] [Hedari et al., ICML 2019]





# high school 2













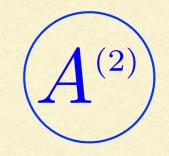
race distribution

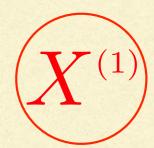


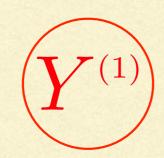
high school 2



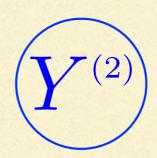
race distribution

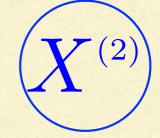






counselors % SAT/ACT-taking







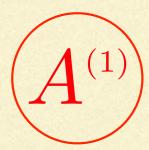




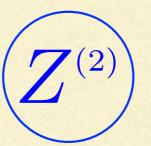
race intervention: distribution calculus classes

intervention: calculus classes

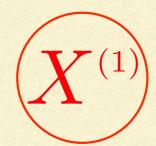
race distribution

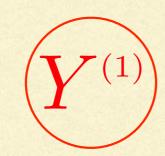


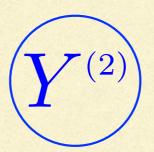


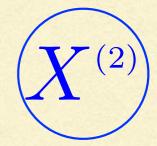












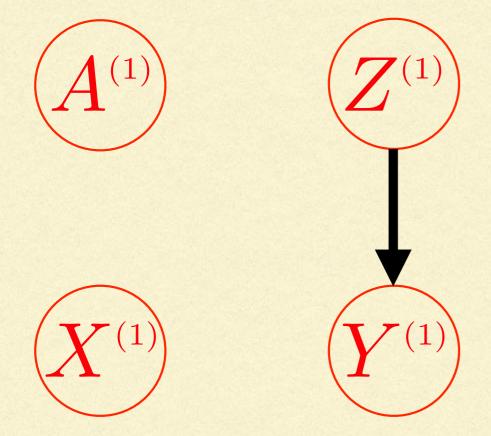
counselors % SAT/ACT-taking

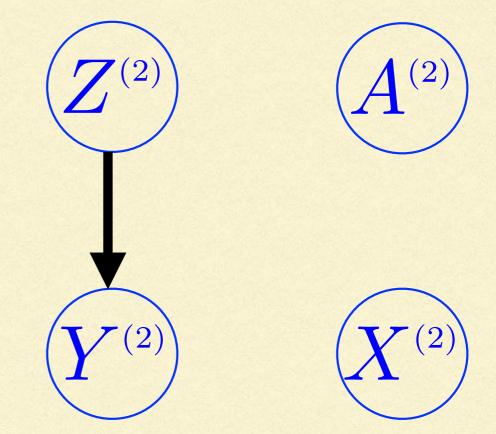




race intervention: distribution calculus classes

intervention: race calculus classes distribution





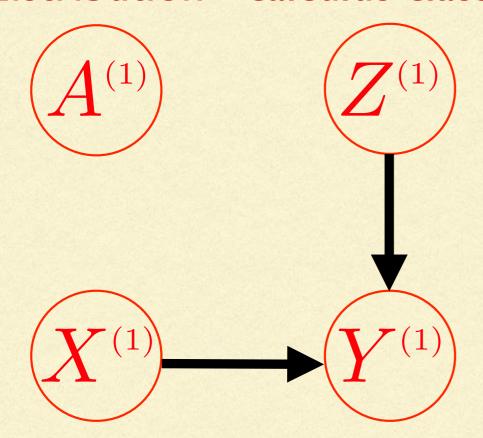
counselors % SAT/ACT-taking

% SAT/ACT-taking counselors

high school 2



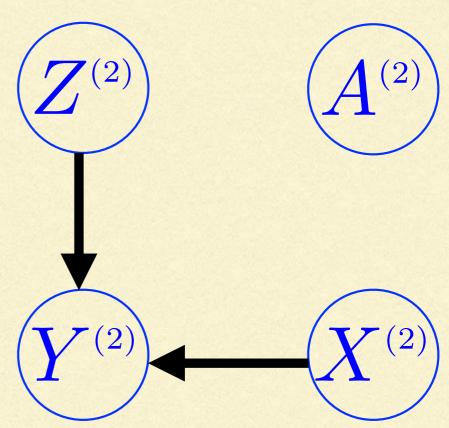
race intervention: distribution calculus classes

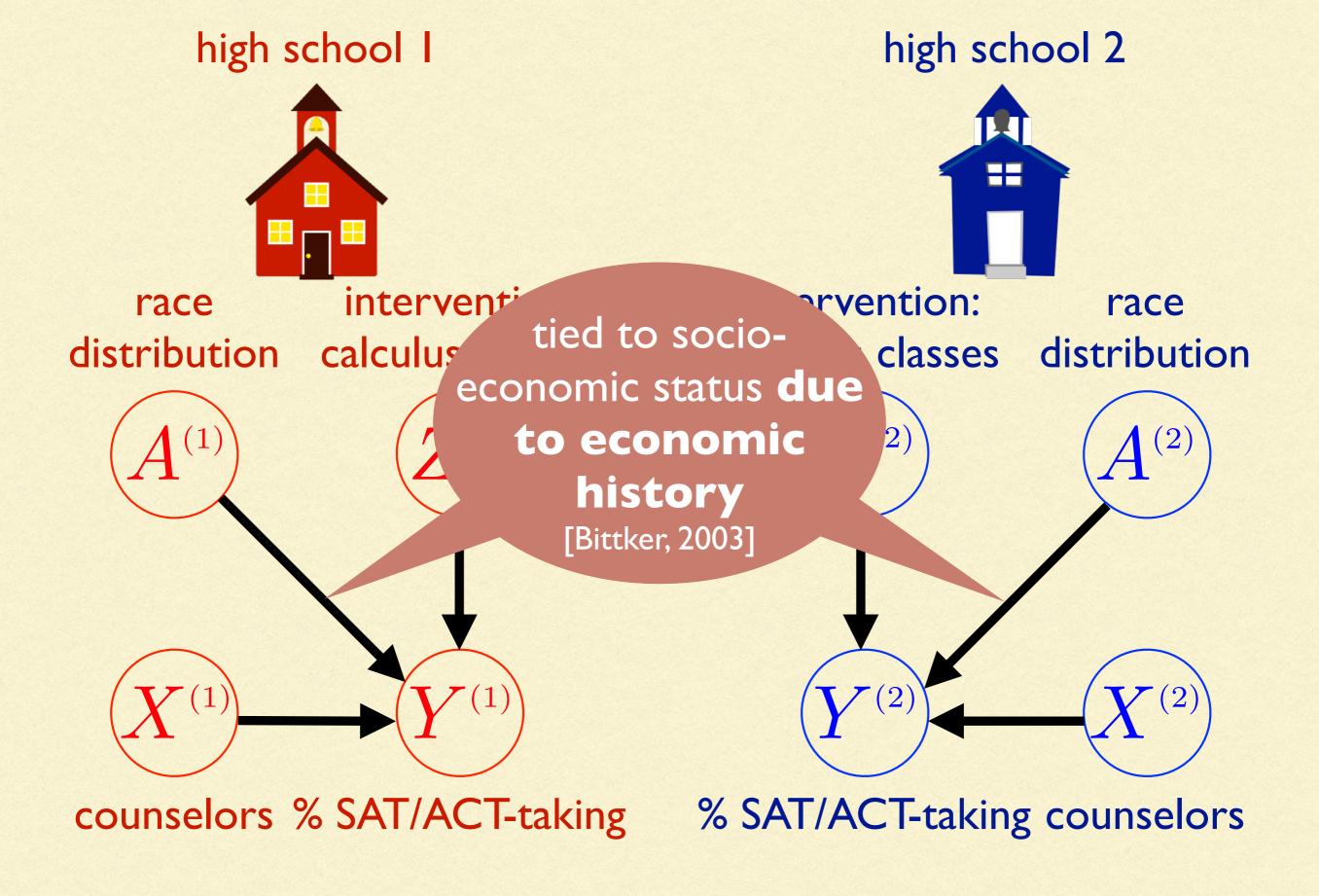


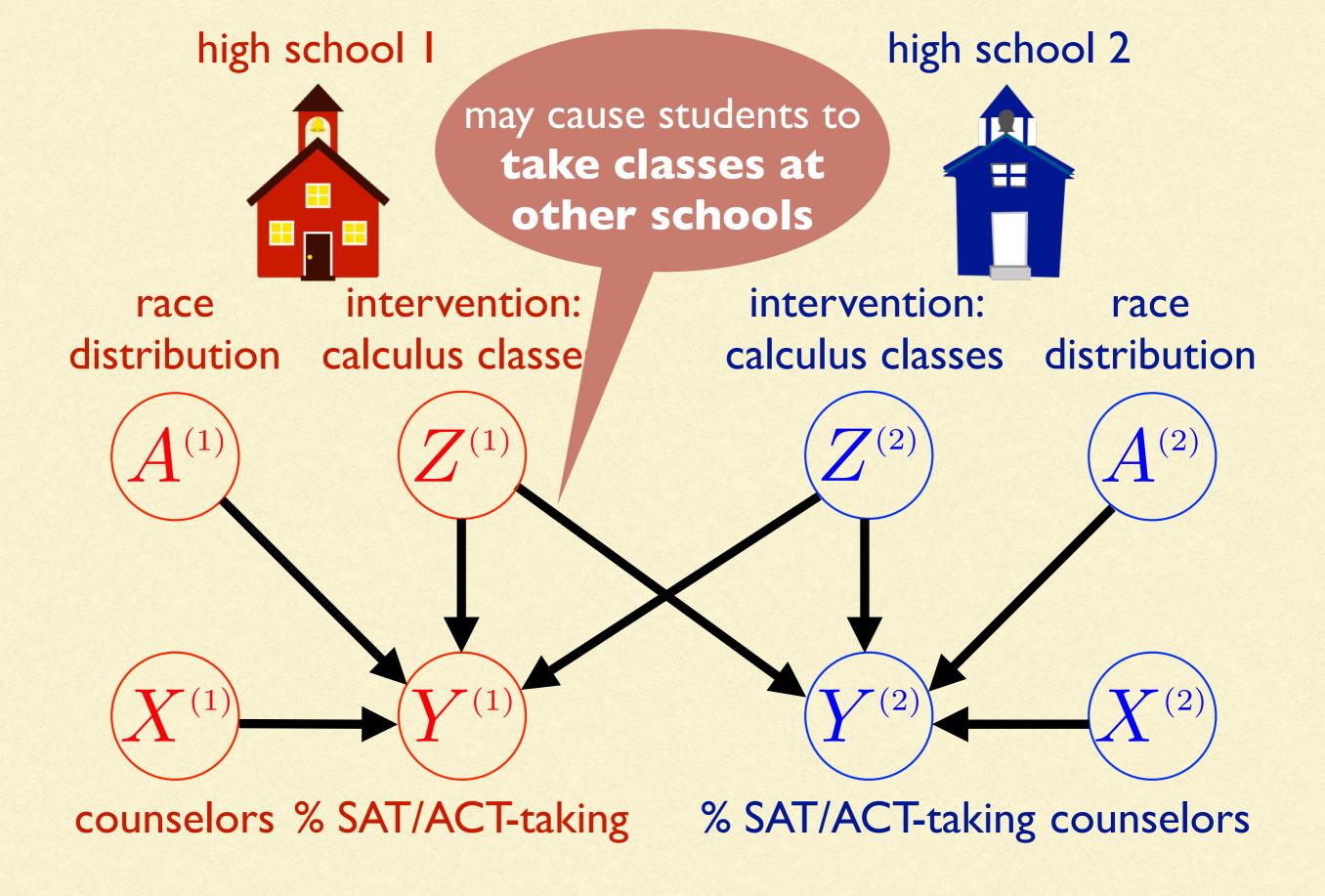
counselors % SAT/ACT-taking



intervention: race calculus classes distribution

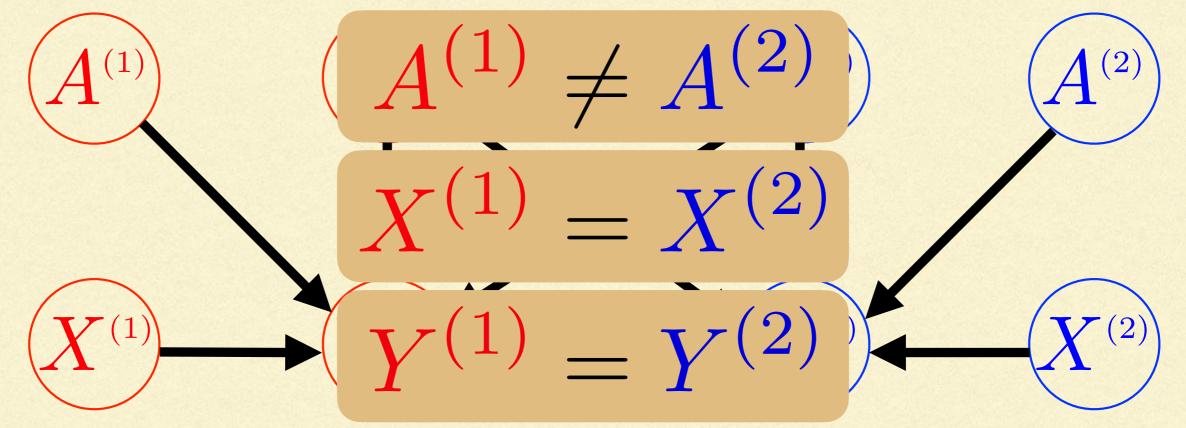






intervention: intervention: race race distribution calculus classes calculus classes distribution (2)(2)counselors % SAT/ACT-taking % SAT/ACT-taking counselors

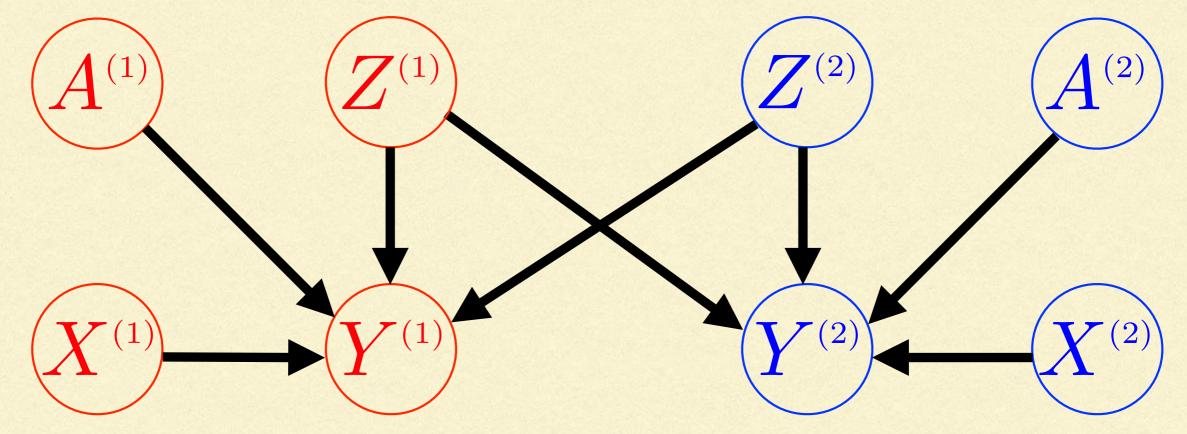
race intervention: intervention: race distribution calculus classes calculus classes distribution



counselors % SAT/ACT-taking

race intervention: distribution calculus classes

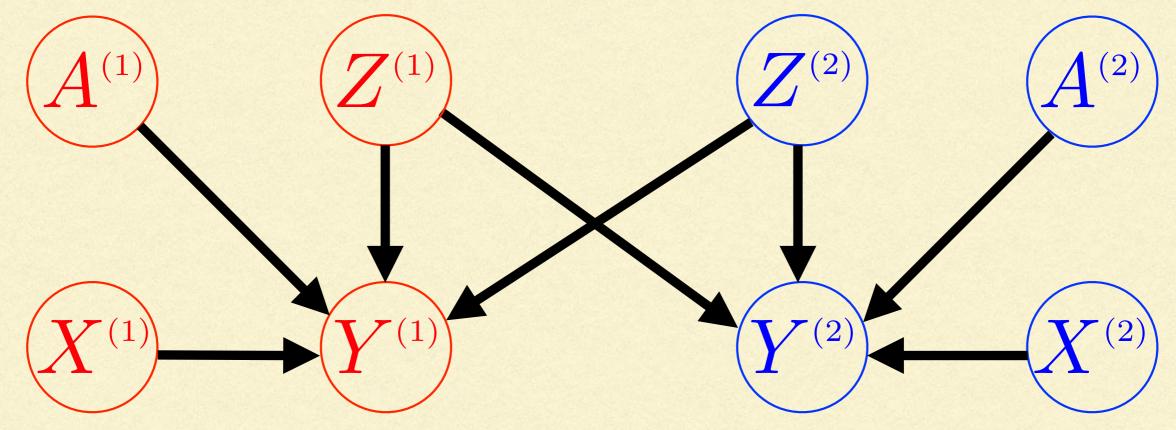
intervention: race calculus classes distribution



counselors % SAT/ACT-taking

$$Y^{(1)}([z^{(1)} = 1, z^{(2)} = 0]) = 1.0$$

race intervention: intervention: race distribution calculus classes calculus classes distribution

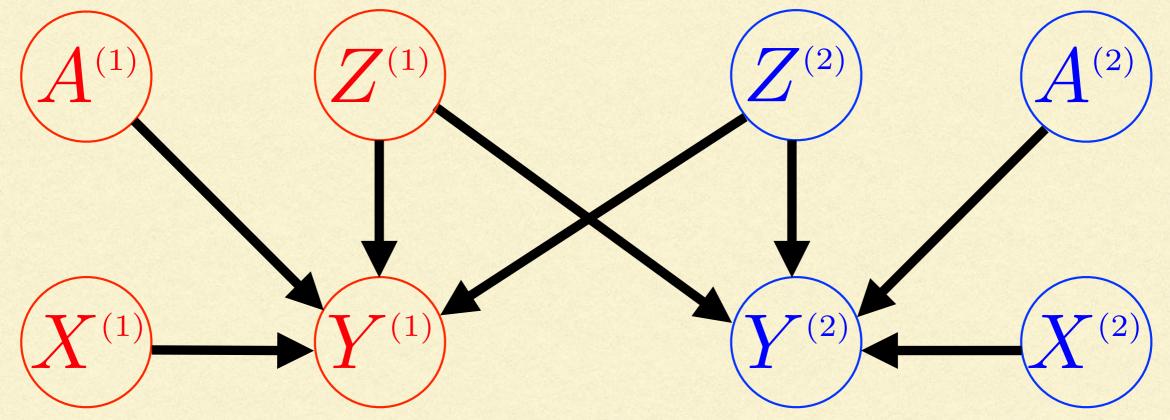


counselors % SAT/ACT-taking

$$Y^{(1)}([z^{(1)} = 1, z^{(2)} = 0]) = 1.0$$

$$Y^{(2)}([z^{(1)} = 1, z^{(2)} = 0]) = 0.1$$

race intervention: intervention: race distribution calculus classes calculus classes distribution



counselors % SAT/ACT-taking

$$Y^{(1)}([z^{(1)} = 1, z^{(2)} = 0]) = 1.0$$

$$Y^{(1)}([z^{(1)} = 0, z^{(2)} = 1]) = 0.6$$

$$Y^{(2)}([z^{(1)} = 1, z^{(2)} = 0]) = 0.1$$

$$Y^{(2)}([z^{(1)} = 0, z^{(2)} = 1]) = 0.5$$

race

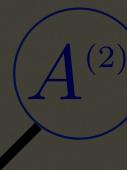
decision: distribution calculus classes

decision: calculus classes distribution

race

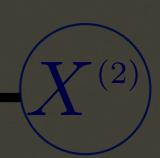


either intervention causes the same average overall impact





but it seems unfair to give classes to school I as they have better impact solely due to race



counselors % SAT/ACT-taking

$$Y^{(1)}([z^{(1)} = 1, z^{(2)} = 0]) = 1.0$$

$$Y^{(2)}([z^{(1)} = 1, z^{(2)} = 0]) = 0.1$$

$$Y^{(1)}([z^{(1)} = 0, z^{(2)} = 1]) = 0.6$$

$$Y^{(2)}([z^{(1)} = 0, z^{(2)} = 1]) = 0.5$$

# MORE FORMALLY

# Maximizing overall impact

$$\max_{\mathbf{z} \in \{0,1\}^n} \sum_{i=1}^n \mathbb{E}[Y^{(i)}(a^{(i)}, \mathbf{z}) \mid A^{(i)} = a^{(i)}, X^{(i)} = \mathbf{x}^{(i)}],$$

$$s.t., \sum_{i=1}^n z^{(i)} \le b$$

# MORE FORMALLY

whether to grant # of schools advanced classes / Maximizing overall impact  $\max_{\mathbf{z} \in \{0,1\}} \sum_{n} \mathbb{E}[Y^{(i)}(a^{(i)}, \mathbf{z}) \mid A^{(i)} = a^{(i)}, X^{(i)} = \mathbf{x}^{(i)}]$ government

budget

$$\mathbb{E}[Y^{(i)}(a^{(i)}, \mathbf{z}) \mid A^{(i)} = a^{(i)}, X^{(i)} = \mathbf{x}^{(i)}]$$

$$\mathbb{E}[Y^{(i)}(a', \mathbf{z}) \mid A^{(i)} = a^{(i)}, X^{(i)} = \mathbf{x}^{(i)}]$$

$$\mathbb{E}[Y^{(i)}(a^{(i)}, \mathbf{z}) \mid A^{(i)} = a^{(i)}, X^{(i)} = \mathbf{x}^{(i)}]$$

$$\mathbb{E}[Y^{(i)}(a', \mathbf{z}) \mid A^{(i)} = a^{(i)}, X^{(i)} = \mathbf{x}^{(i)}]$$

#### a counterfactual:

impact school i would have gotten for interventions **z** if race distribution was a'

$$\mathbb{E}[Y^{(i)}(a^{(i)}, \mathbf{z}) \mid A^{(i)} = a^{(i)}, X^{(i)} = \mathbf{x}^{(i)}] - \mathbb{E}[Y^{(i)}(a', \mathbf{z}) \mid A^{(i)} = a^{(i)}, X^{(i)} = \mathbf{x}^{(i)}] < \tau$$

#### a counterfactual:

impact school i would have gotten for interventions **z** if race distribution was a'

## constraint on counterfactual privilege

$$\mathbb{E}[Y^{(i)}(a^{(i)}, \mathbf{z}) \mid A^{(i)} = a^{(i)}, X^{(i)} = \mathbf{x}^{(i)}] \\ - \mathbb{E}[Y^{(i)}(a', \mathbf{z}) \mid A^{(i)} = a^{(i)}, X^{(i)} = \mathbf{x}^{(i)}] < \tau$$

#### a counterfactual:

impact school i would have gotten for interventions **z** if race distribution was a'

# MORE FORMALLY

# Maximizing impact with privilege constraints

$$\max_{\mathbf{z} \in \{0,1\}^n} \sum_{i=1}^n \mathbb{E}[Y^{(i)}(a^{(i)}, \mathbf{z}) \mid A^{(i)} = a^{(i)}, X^{(i)} = \mathbf{x}^{(i)}]$$

$$s.t., \sum_{i=1}^{n} z^{(i)} \le b$$

$$c_{ia'} \leq \tau \quad \forall a' \in \mathcal{A}, i \in \{1, \dots, n\},$$

$$\mathbb{E}[Y^{(i)}(a^{(i)}, \mathbf{z}) \mid A^{(i)} = a^{(i)}, X^{(i)} = \mathbf{x}^{(i)}] \\ - \mathbb{E}[Y^{(i)}(a', \mathbf{z}) \mid A^{(i)} = a^{(i)}, X^{(i)} = \mathbf{x}^{(i)}]$$

$$\mathbb{E}[Y^{(i)}(a^{(i)}, \mathbf{z}) \mid A^{(i)} = a^{(i)}, X^{(i)} = \mathbf{x}^{(i)}] \\ - \mathbb{E}[Y^{(i)}(a', \mathbf{z}) \mid A^{(i)} = a^{(i)}, X^{(i)} = \mathbf{x}^{(i)}] < \tau$$

$$\tau = 0$$

$$Y^{(1)}([z^{(1)} = 1, z^{(2)} = 0]) = 1.0$$
  $Y^{(2)}([z^{(1)} = 1, z^{(2)} = 0]) = 0.1$   $Y^{(1)}([z^{(1)} = 0, z^{(2)} = 1]) = 0.6$   $Y^{(2)}([z^{(1)} = 0, z^{(2)} = 1]) = 0.5$ 

high school I

$$\mathbb{E}[Y^{(i)}(a^{(i)}, \mathbf{z}) \mid A^{(i)} = a^{(i)}, X^{(i)} = \mathbf{x}^{(i)}] \\ - \mathbb{E}[Y^{(i)}(a', \mathbf{z}) \mid A^{(i)} = a^{(i)}, X^{(i)} = \mathbf{x}^{(i)}] < \tau$$

$$\tau = 0$$

essentially counterfactuals!

$$Y^{(1)}([z^{(1)} = 1, z^{(2)} = 0]) = 1.0$$
  $Y^{(2)}([z^{(1)} = 1, z^{(2)} = 0]) = 0.1$ 

$$Y^{(1)}([z^{(1)} = 0, z^{(2)} = 1]) = 0.6$$
  $Y^{(2)}([z^{(1)} = 0, z^{(2)} = 1]) = 0.5$ 

high school I

$$\mathbb{E}[Y^{(i)}(a^{(i)}, \mathbf{z}) \mid A^{(i)} = a^{(i)}, X^{(i)} = \mathbf{x}^{(i)}] \\ - \mathbb{E}[Y^{(i)}(a', \mathbf{z}) \mid A^{(i)} = a^{(i)}, X^{(i)} = \mathbf{x}^{(i)}] < \tau$$

$$\tau = 0$$

$$Y^{(1)}([z^{(1)} = 1, z^{(2)} = 0])$$
  
-  $Y^{(2)}([z^{(1)} = 1, z^{(2)} = 0]) = 0.9$ 

$$Y^{(1)}([z^{(1)} = 1, z^{(2)} = 0]) = 1.0$$
  $Y^{(2)}([z^{(1)} = 1, z^{(2)} = 0]) = 0.1$ 

$$Y^{(2)}([z^{(1)} = 1, z^{(2)} = 0]) = 0.1$$

$$Y^{(1)}([z^{(1)} = 0, z^{(2)} = 1]) = 0.6$$

$$Y^{(1)}([z^{(1)} = 0, z^{(2)} = 1]) = 0.6$$
  $Y^{(2)}([z^{(1)} = 0, z^{(2)} = 1]) = 0.5$ 

high school I

$$\mathbb{E}[Y^{(i)}(a^{(i)}, \mathbf{z}) \mid A^{(i)} = a^{(i)}, X^{(i)} = \mathbf{x}^{(i)}] \\ - \mathbb{E}[Y^{(i)}(a', \mathbf{z}) \mid A^{(i)} = a^{(i)}, X^{(i)} = \mathbf{x}^{(i)}] < \tau$$

$$\tau = 0$$

$$Y^{(1)}([z^{(1)} = 1, z^{(2)} = 0])$$

$$-Y^{(2)}([z^{(1)} = 1, z^{(2)} = 0]) = 0.9$$

$$Y^{(2)}([z^{(1)} = 0, z^{(2)} = 1])$$
  
-  $Y^{(1)}([z^{(1)} = 0, z^{(2)} = 1]) = -0.1$ 

$$Y^{(1)}([z^{(1)} = 1, z^{(2)} = 0]) = 1.0$$
  $Y^{(2)}([z^{(1)} = 1, z^{(2)} = 0]) = 0.1$ 

$$Y^{(2)}([z^{(1)} = 1, z^{(2)} = 0]) = 0.1$$

$$(Y^{(1)}([z^{(1)} = 0, z^{(2)} = 1]) = 0.6)$$
  $(Y^{(2)}([z^{(1)} = 0, z^{(2)} = 1]) = 0.5)$ 

$$Y^{(2)}([z^{(1)} = 0, z^{(2)} = 1]) = 0.5$$

high school I

$$\mathbb{E}[Y^{(i)}(a^{(i)}, \mathbf{z}) \mid A^{(i)} = a^{(i)}, X^{(i)} = \mathbf{x}^{(i)}] \\ - \mathbb{E}[Y^{(i)}(a', \mathbf{z}) \mid A^{(i)} = a^{(i)}, X^{(i)} = \mathbf{x}^{(i)}] < \tau$$

$$\tau = 0$$

$$Y^{(1)}([z^{(1)} = 1, z^{(2)} = 0])$$

$$-Y^{(2)}([z^{(1)} = 1, z^{(2)} = 0]) = 0.9$$



school 2 gets classes

$$Y^{(2)}([z^{(1)} = 0, z^{(2)} = 1])$$
 $-Y^{(1)}([z^{(1)} = 0, z^{(2)} = 1]) = -0.1$ 



$$Y^{(1)}([z^{(1)} = 1, z^{(2)} = 0]) = 1.0$$

$$Y^{(2)}([z^{(1)} = 1, z^{(2)} = 0]) = 0.1$$

$$Y^{(1)}([z^{(1)} = 0, z^{(2)} = 1]) = 0.6$$
  $Y^{(2)}([z^{(1)} = 0, z^{(2)} = 1]) = 0.5$ 

$$Y^{(2)}([z^{(1)} = 0, z^{(2)} = 1]) = 0.5$$

high school I

#### VS. COUNTERFACTUAL FAIRNESS

#### constraint on counterfactual privilege

$$\mathbb{E}[Y^{(i)}(a^{(i)}, \mathbf{z}) \mid A^{(i)} = a^{(i)}, X^{(i)} = \mathbf{x}^{(i)}] - \mathbb{E}[Y^{(i)}(a', \mathbf{z}) \mid A^{(i)} = a^{(i)}, X^{(i)} = \mathbf{x}^{(i)}] < \tau$$

VS.

$$P(\hat{Y}^{(i)}(a^{(i)}) = y \mid A^{(i)} = a^{(i)}, X^{(i)} = \mathbf{x}^{(i)})$$

$$= P(\hat{Y}^{(i)}(a') = y \mid A^{(i)} = a^{(i)}, X^{(i)} = \mathbf{x}^{(i)})$$

#### counterfactual fairness

[Kusner et al., 2017]

## OPTIMIZATION: MILP

$$\max_{\mathbf{z} \in \{0,1\}^n} \sum_{i=1}^n \sum_{j=1}^{2^K} h_{ij} \xi^{ij}(a^{(i)})$$

$$\mathbf{s}.t., \sum_{j=1}^{2^K} h_{i,j} \left[ \xi_{\prec}^{ij}(a^{(i)}) - \xi_{\prec}^{ij}(a') \right] < \tau, \quad \forall a', i$$

$$\mathbb{I}[\mathbf{e}_j = 1] h_{ij} \leq \mathbf{z}^{N(i)}, \qquad \forall i, j$$

$$\mathbb{I}[\mathbf{e}_j = 0] h_{ij} \leq 1 - \mathbf{z}^{N(i)}, \qquad \forall i, j$$

$$\sum_{j=1}^{2^K} h_{ij} = 1, \qquad \forall i$$

$$\sum_{i=1}^n z^{(i)} \leq b.$$

## OPTIMIZATION: MII P

can accommodate any

$$\max_{\mathbf{z} \in \{0,1\}^n \atop \mathbf{H} \in [0,1]^{(n,2^K)}} \sum_{i=1}^n \sum_{j=1}^{2^K} h_{ij} \xi^{ij}(a^{(i)}) \text{ formulation of impact } \\ \xi^{ij}(a^{(i)}) := \mathbb{E}[Y^{(i)}(a^{(i)}, \mathbf{z}) \mid A^{(i)} = a^{(i)}, X^{(i)} = \mathbf{x}^{(i)}]$$

$$\{\xi^{ij}(a^{(i)}) := \mathbb{E}[Y^{(i)}(a^{(i)}, \mathbf{z}) \mid A^{(i)} = a^{(i)}, X^{(i)} = \mathbf{x}^{(i)}]$$

$$s.t., \sum_{j=1}^{2^K} h_{i,j} \left[ \xi_{\prec}^{ij}(a^{(i)}) - \xi_{\prec}^{ij}(a') \right] < \tau, \quad \forall a', i$$

$$\mathbb{I}[\mathbf{e}_j = 1] h_{ij} \le \mathbf{z}^{N(i)}, \qquad \forall i, j$$

$$\mathbb{I}[\mathbf{e}_j = 0]h_{ij} \le 1 - \mathbf{z}^{N(i)}, \qquad \forall i, j$$

$$\sum_{i=1}^{2^K} h_{ij} = 1, \qquad \forall i$$

$$\sum_{i=1}^{n} z^{(i)} \le b.$$

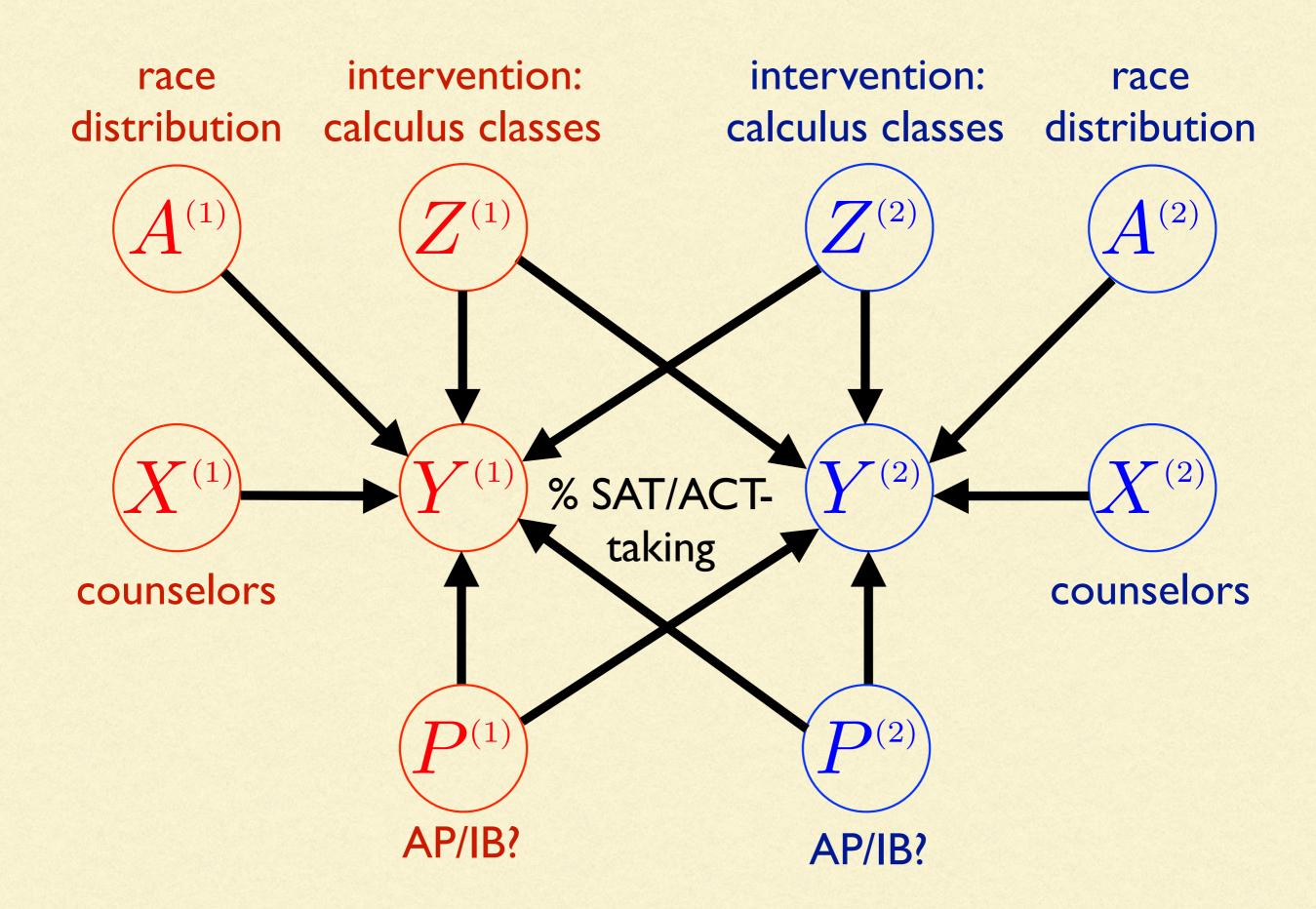
# NYC PUBLIC SCHOOL FUNDING

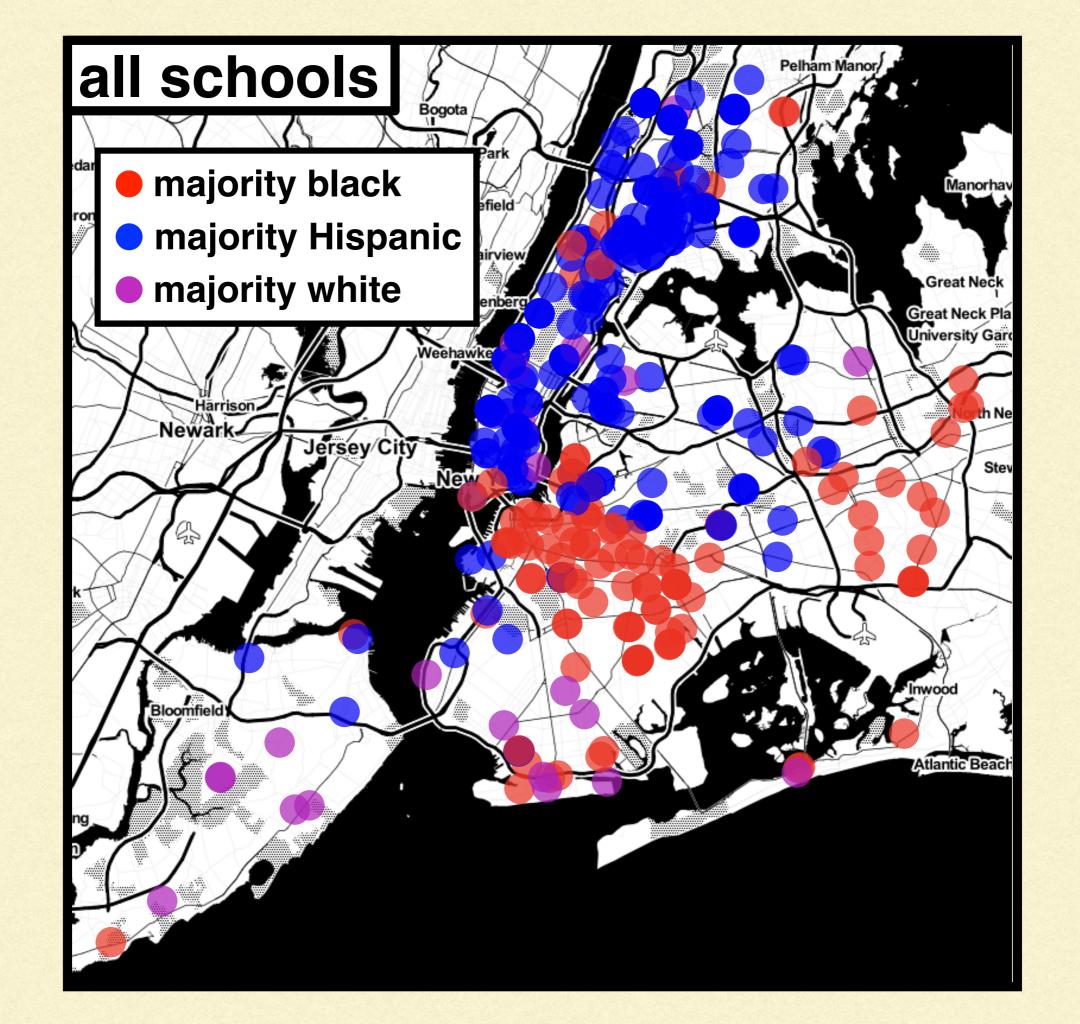
[CRDC, HTTPS://OCRDATA.ED.GOV/]

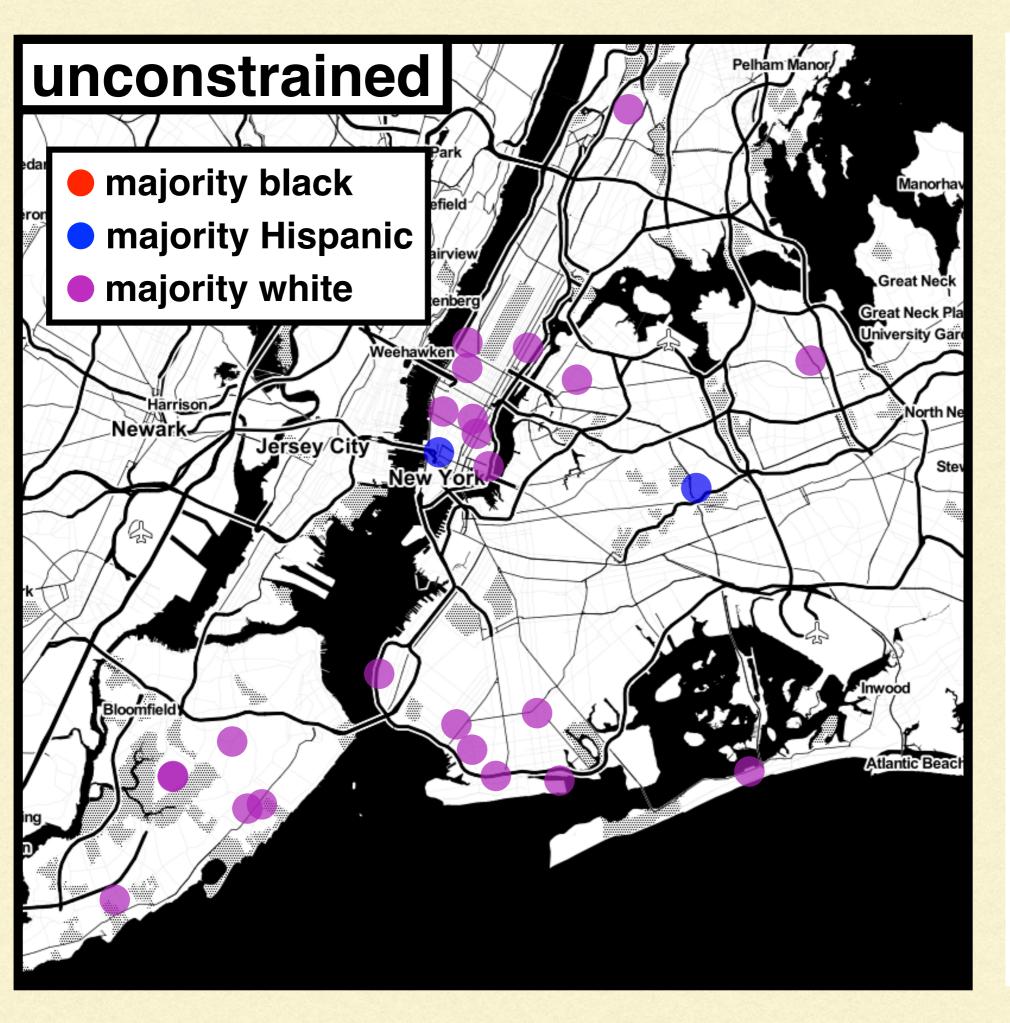
#### 345 schools

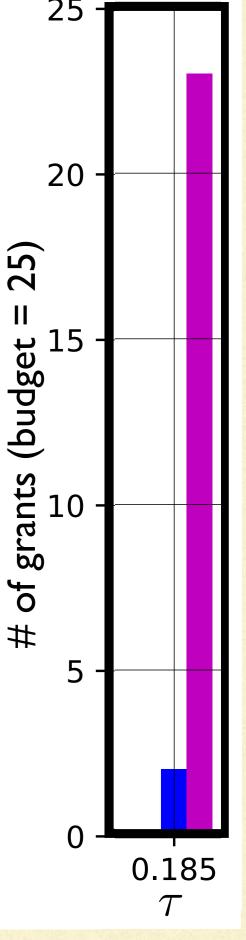


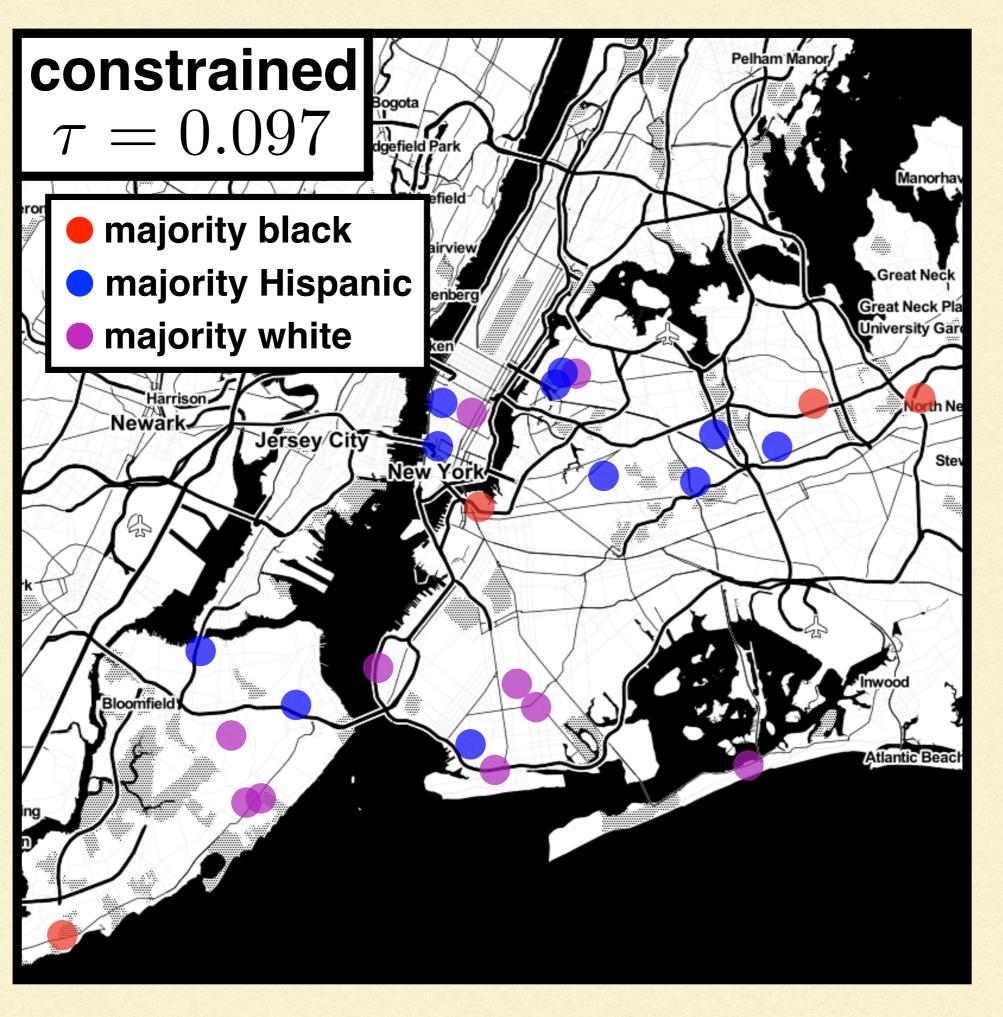
school I school 2

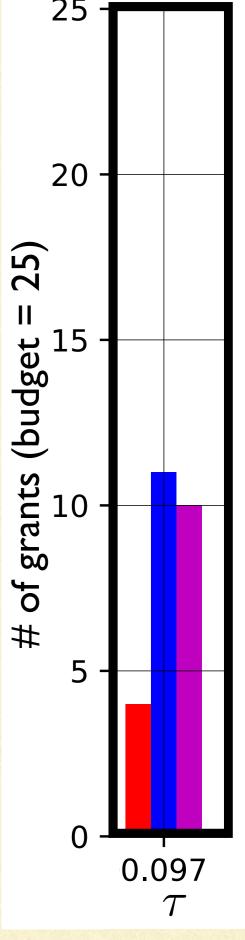


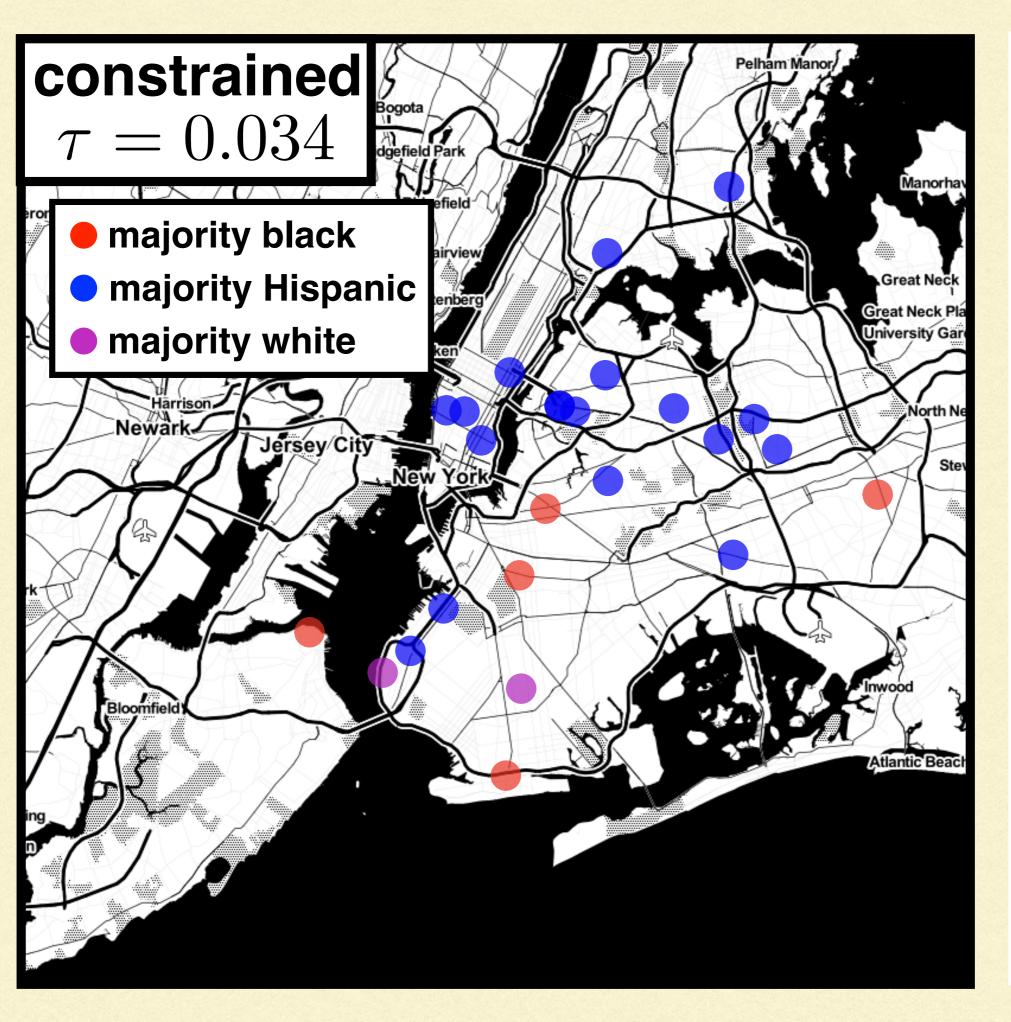


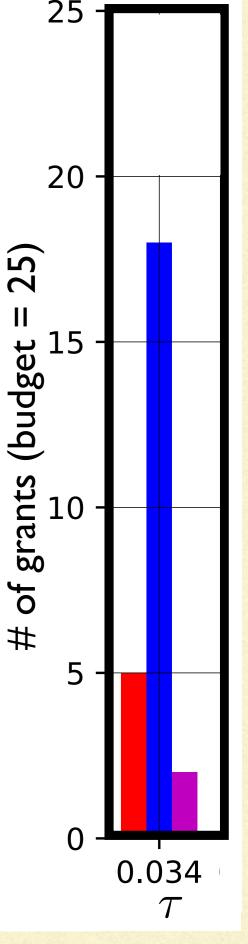


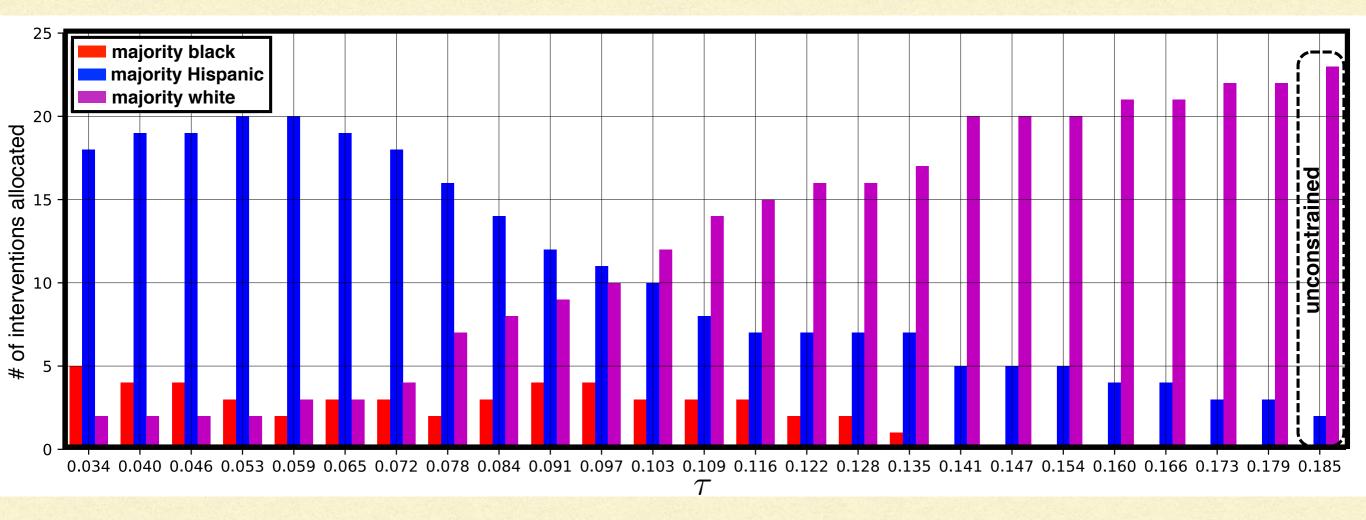


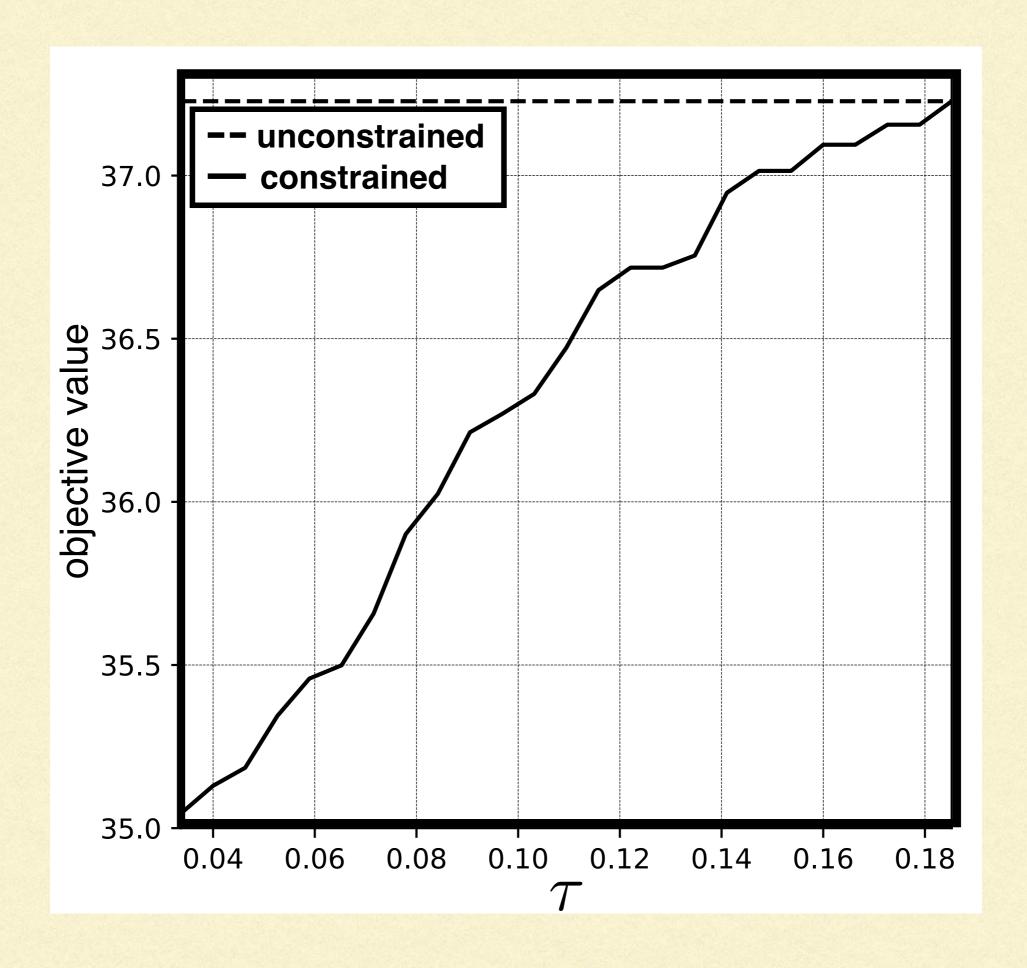


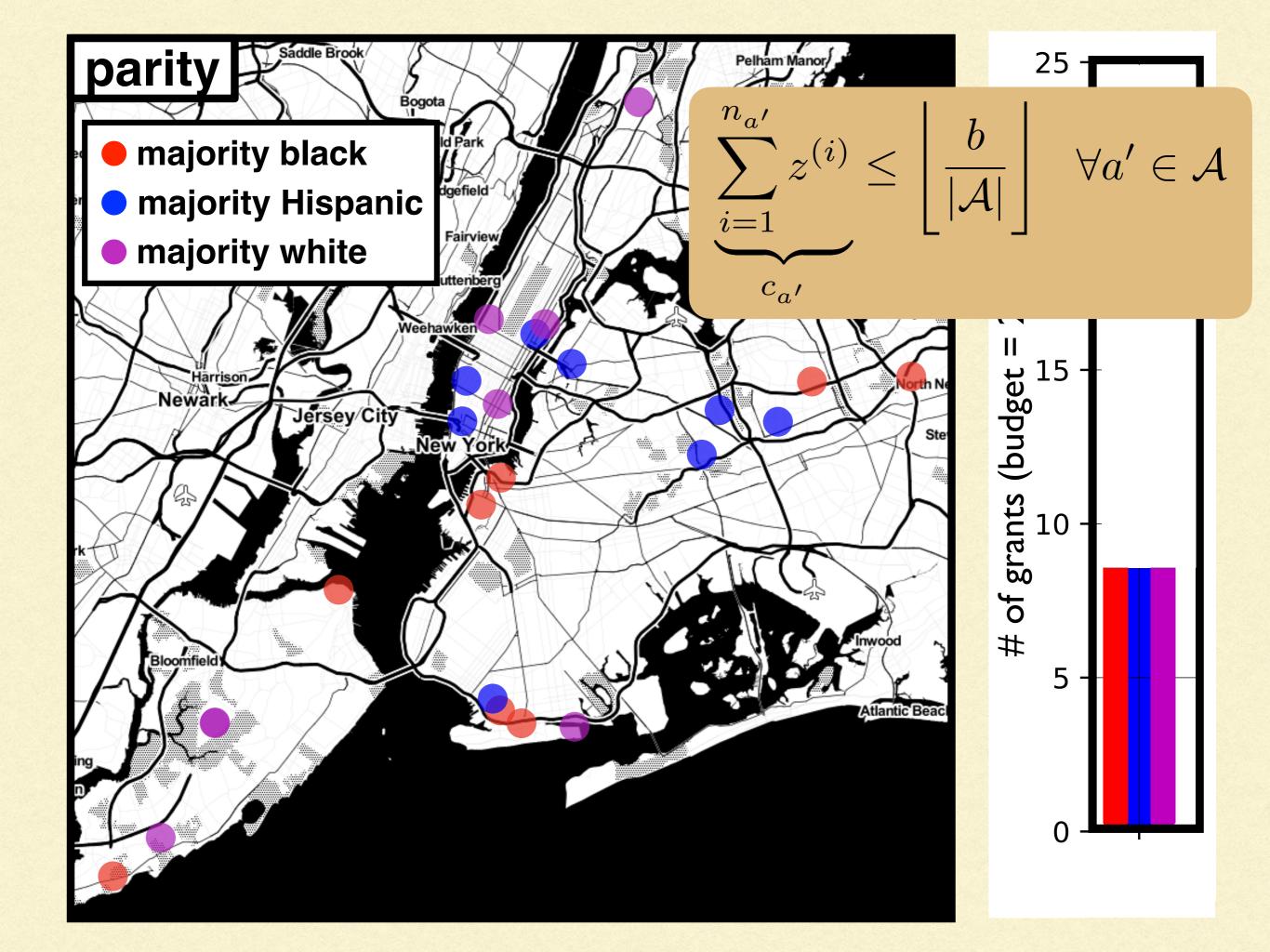


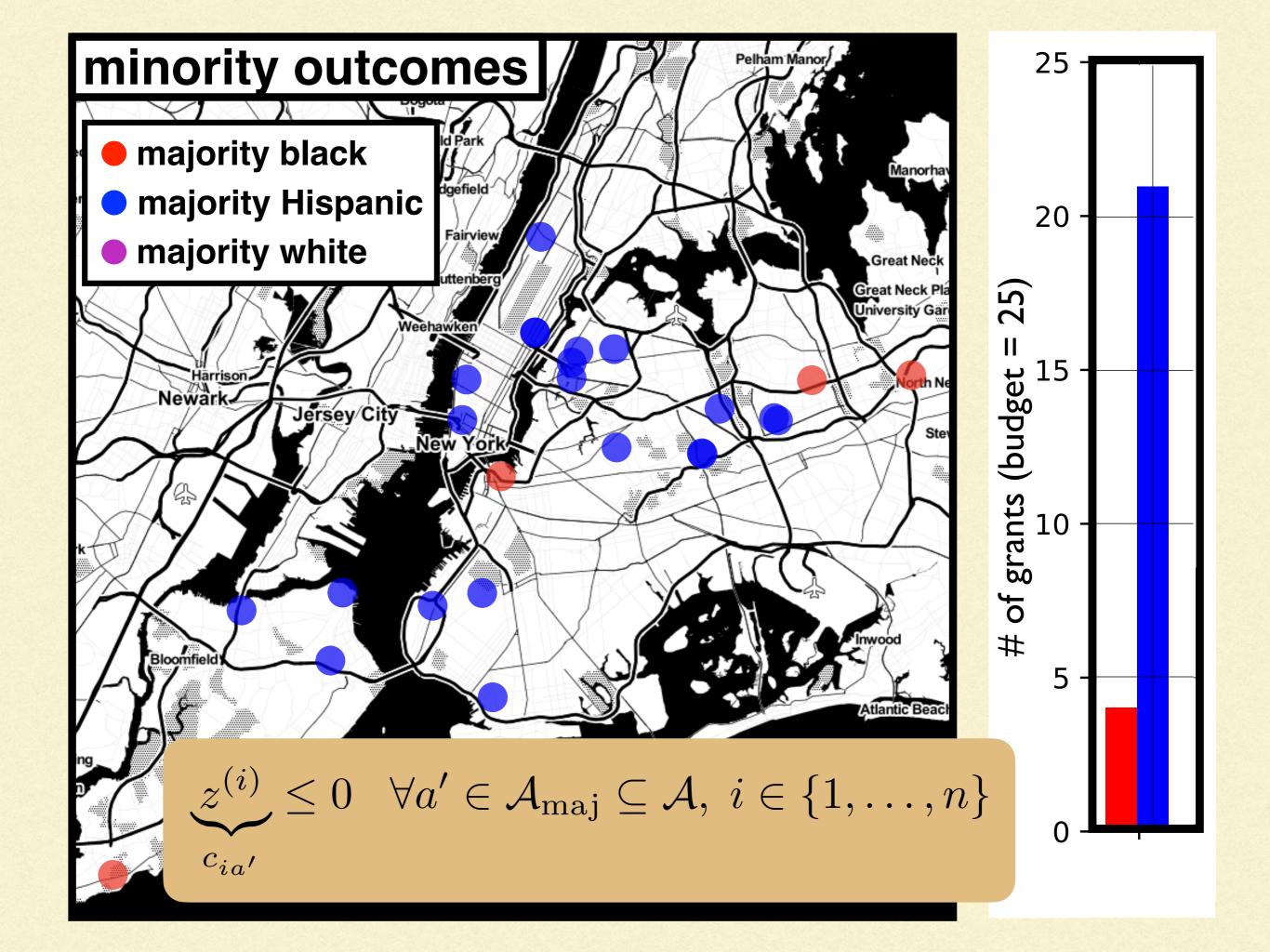


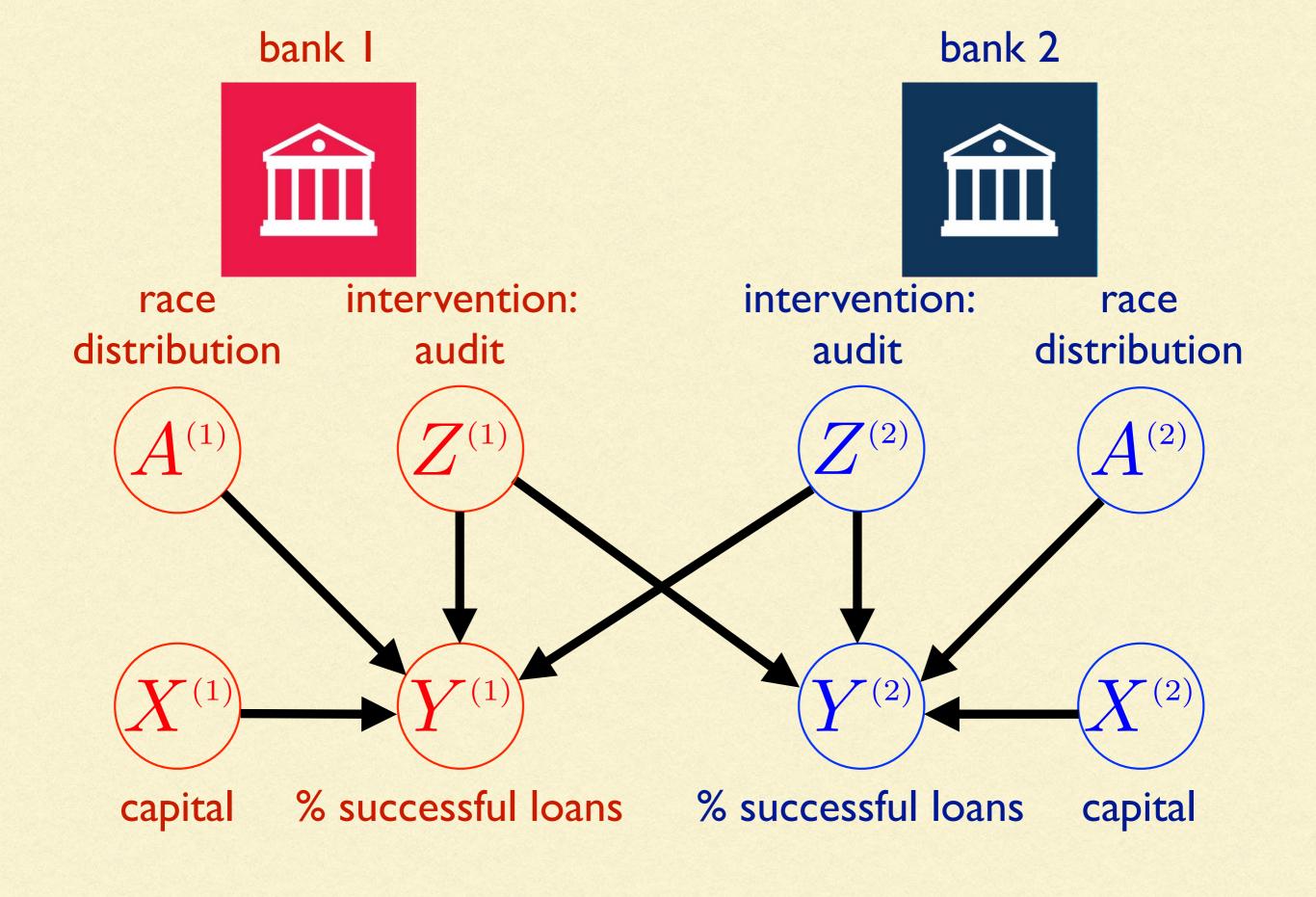










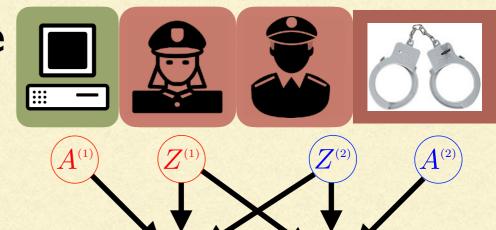


 Many cases where ML algorithms decide only part of an impact



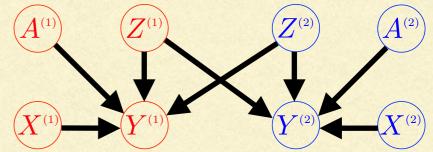


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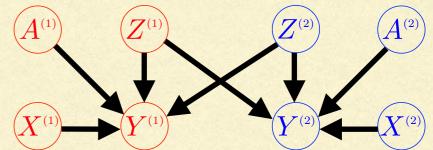




$$Y^{(1)}([z^{(1)} = 1, z^{(2)} = 0])$$
$$-Y^{(2)}([z^{(1)} = 1, z^{(2)} = 0]) = 0.9$$

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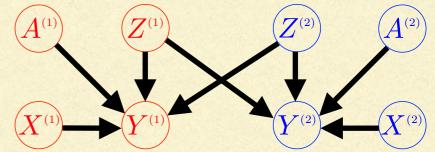
$$\max_{\mathbf{z} \in \{0,1\}^n} \sum_{i=1}^n \mathbb{E}[Y^{(i)}(a^{(i)}, \mathbf{z}) \mid A^{(i)} = a^{(i)}, X^{(i)} = \mathbf{x}^{(i)}]$$

$$s.t., \sum_{i=1}^n z^{(i)} \le b$$

$$c_{ia'} \le \tau \quad \forall a' \in \mathcal{A}, i \in \{1, \dots, n\},$$

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- Allows one to make less discriminatory policy decisions for school funding



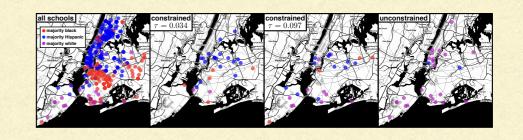


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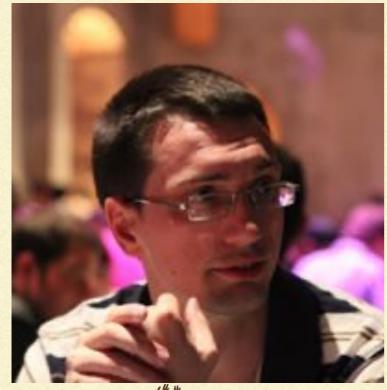
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