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Bitcoin's Fatal Flaw: The Limited Adoption Problem

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Discussion by Katya Malinova

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Brief Summary

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- Blockchain as payment infrastructure
- Bitcoin (proof-of-work) blockchain is not scalable
 - Limited adoption: the fraction of users who use the blockchain for payments vanishes as the number of users increases
- Permissioned blockchain is a viable alternative
 - But not for all consensus mechanisms, e.g.:
 - simple majority voting doesn't work
 - voting scaled by crypto-currency holdings does

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"Traditional" payment system

- unmodelled
- normalized as zero reward, zero cost?

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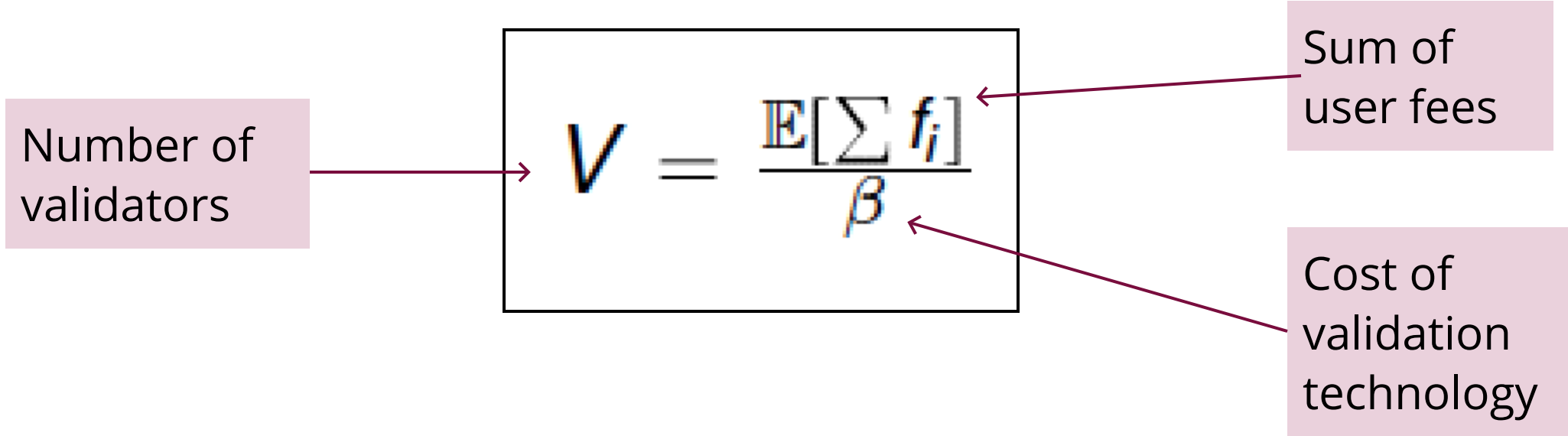
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Sum of
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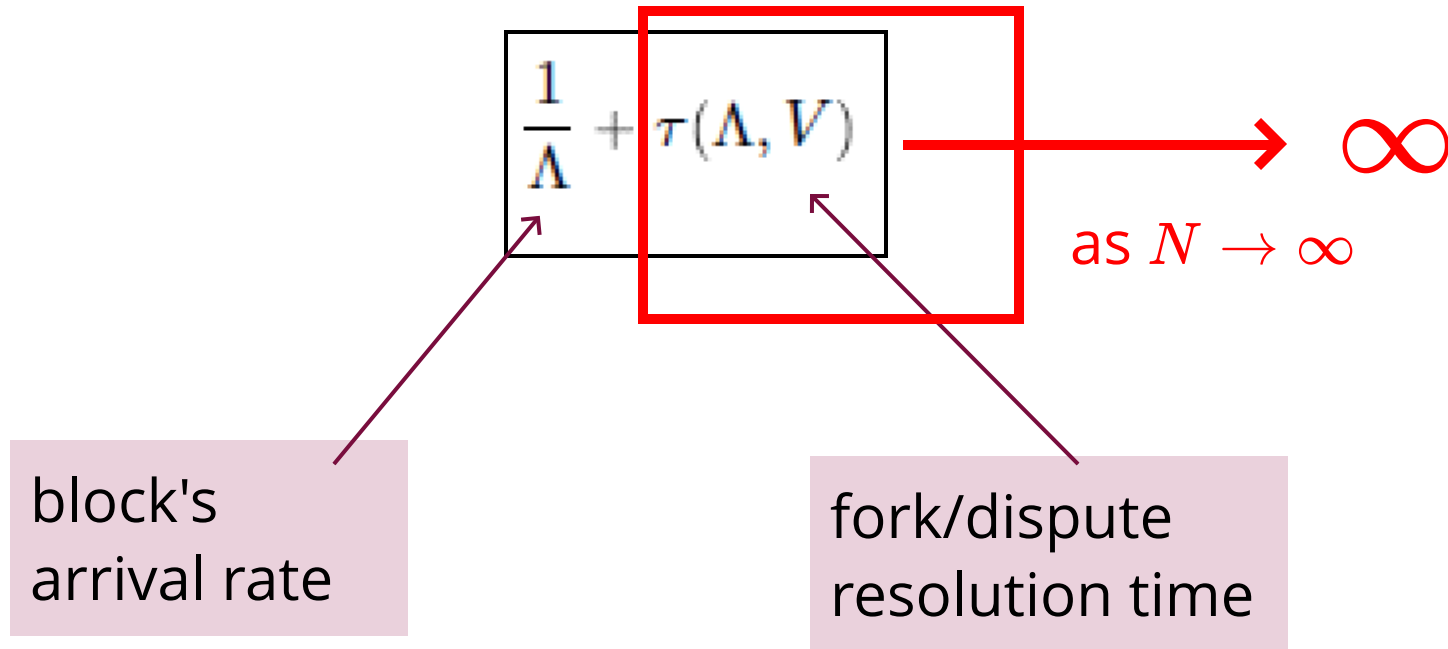
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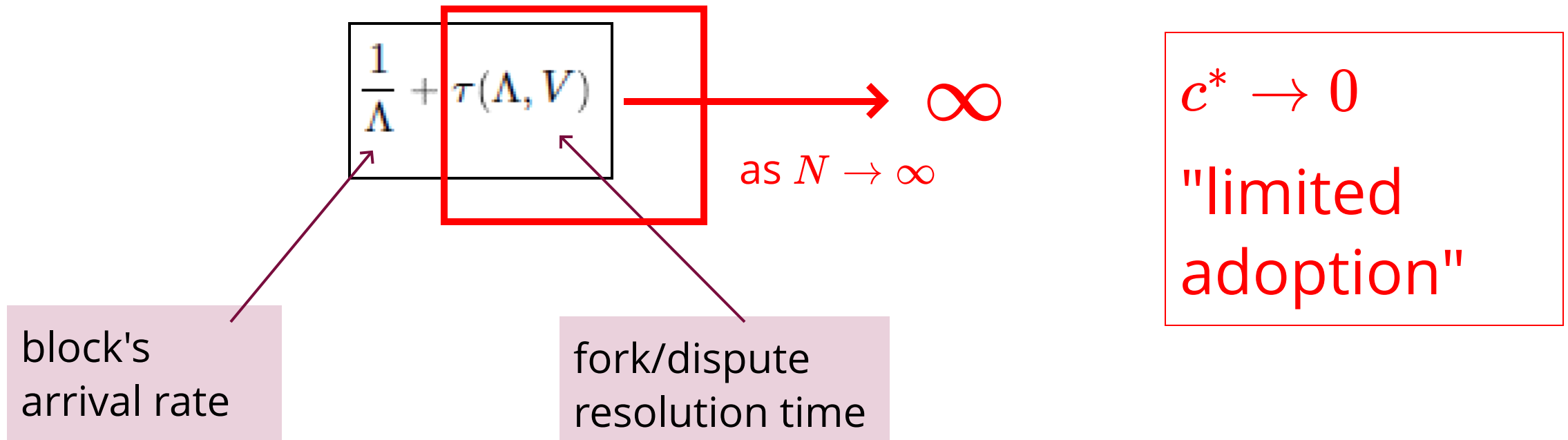
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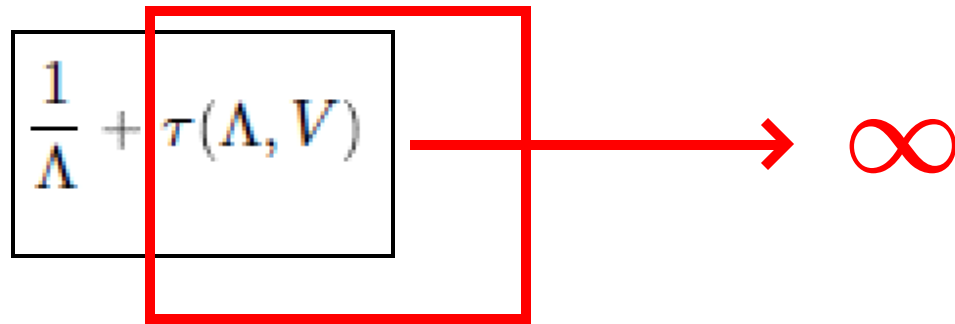


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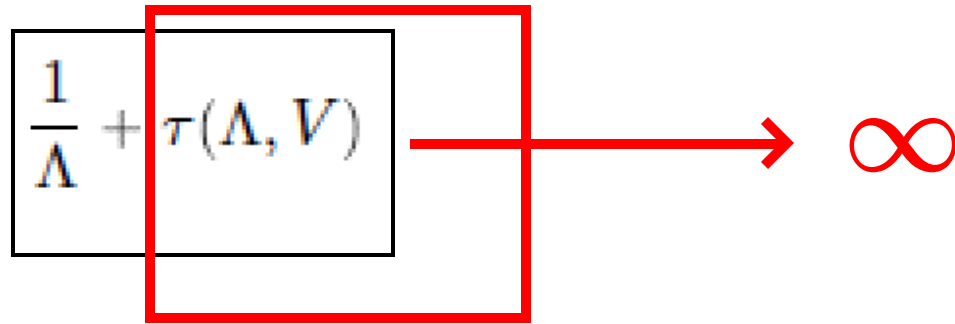


Comments/Questions:

$$\frac{1}{\Lambda} + \tau(\Lambda, V) \rightarrow \infty$$


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Network delay/physical system limits

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Lemma B.1 in
Appendix B

Network delay/physical system limits

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Comment 1: need more intuition for this:

- User i pays fee $f_i \propto (N - 1)c_i^2$
- With $N \rightarrow \infty$, wait times explode & only super-patient users use blockchain ...
 - $\rightarrow c_i \approx 0$
- Fraction of blockchain users vanishes ...
- What happens to fee per user?

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Comment 2:

- Confirmation times $\rightarrow \infty$
 \Rightarrow fees are received with infinite delay
- Technology costs are incurred in real time! (?)
- Are validators infinitely patient? No capital constraints?
 - Is there a transversality condition?

Model 2: (Permissioned Blockchain)

Users:

- same as before

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- Finite number
- Play a coordination game, choose:
 - be malicious
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- Finite number
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- Where does the reward come from?
- Seemingly should depend on the value of transactions and/or malicious users?

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This paper: 2.5 models

1. Proof-of-Work -- validators' incentives unmodelled
2. Permissioned -- coordination game among validators
 - with majority voting
 - with crypto-currency stake-weighted voting
 - → must introduce and value cryptocurrency

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 - → must introduce and value cryptocurrency

No clear connection between #1 and #2

- Why move from decentralized proof-of-work to permissioned?
- Are there decentralized alternatives?
 - E.g., require minimum crypto-stake to become a validator?

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Where does the utility gain from blockchain use stem from?

- E.g., with bitcoin: censorship-resistance, immutability ...
- But this disappears if blockchain is permissioned

Question: purpose of a blockchain in the model?

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- similar reward structure for permissionless PoW vs. permissioned

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Key differences (from the user perspective) b/n the permissioned blockchain vs. traditional payment system in the model?

- Central Bank Digital Currency?

Suggestion: better connections to existing literature

Various "impossibility triangles" have been discussed:

- The authors mention Buterin's: scalability, security, decentralization triangle
- This is also discussed in the academic literature, e.g.:
 - comp sci: Gilbert and Lynch (2002)
 - econ&finance: Abadi and Brunermeier (2018)
 - see Chen, Cong, Xiao (2019) for a survey

Suggestion: better connections to existing literature

- The paper:
 - co-existence of payment and currency systems
 - role for the value of cryptocurrency (for the voting weights)
 - users don't directly affect crypto-valuation

- Is this approach consistent with the predictions from the user-driven cryptocurrency valuation models, where value is affected by e.g.:
 - possible speculation
 - coordination among users
 - see Malinova (2019) for a survey



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